

# THE EUROPEAN DIRECTORATE FOR THE QUALITY OF MEDICINES & HEALTHCARE (EDQM)



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# CombiStats online Training module 3

## Assays based on quantitative responses

# Content

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- Introduction
- Parallel-line analysis
- Slope-ratio analysis
- 4-parameter logistic model
- 5-parameter logistic model
- 3-parameter exponential model

# Indirect dilution assay

## Common structure

- X = several preparations & doses
- Y = single or repeated measurements

## Regression models in CombiStats

$$Y = f(X)$$

### Quantitative responses

Y = continuous/discrete data  
E.g. ELISA (absorbance)

Doses	(1)	(2)
1/10	2.912	2.917
1/20	2.579	2.654
1/40	2.130	2.212
1/80	1.651	1.638
1/160	1.073	0.973
1/320	0.585	0.666
1/640	0.463	0.356
1/1280	0.266	0.234
1/2560	0.228	0.197
1/5120	0.176	0.215

## Ph. Eur. Chapter 5.3 Statistical analysis of results of biological assays and tests

1. introduction
2. randomisation and independence of individual treatments
3. assays depending upon **quantitative responses**
  - 3.2. the parallel-line model
  - 3.3. the slope-ratio model
  - 3.4. extended sigmoid dose-response curves
4. assays depending upon **quantal responses**
  - 4.2. the probit method
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  - 4.5. the median effective dose
5. examples
6. **combination of assay results**
  - 6.2. combination of independent assay results
  - 6.3. unweighted combination of assay results
7. beyond this annex
8. tables and generating procedures
9. glossary of symbols
10. literature

# Application

## Several preparations

**Ref. preparation**  
known concentration

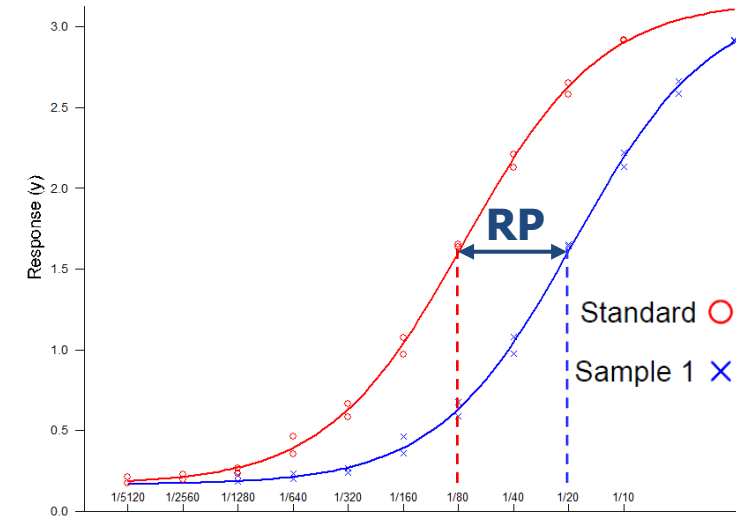
Standard			
Ass. pot.	0.4 IU/ml		
Doses	(1)	(2)	
1/10	2.912	2.917	2.915
1/20	2.579	2.654	2.617
1/40	2.130	2.212	2.171
1/80	1.651	1.638	1.645
1/160	1.073	0.973	1.023
1/320	0.585	0.666	0.626
1/640	0.463	0.356	0.410
1/1280	0.266	0.234	0.250
1/2560	0.228	0.197	0.213
1/5120	0.176	0.215	0.196

**Test preparation(s)**  
conc. to be determined

Sample 1			
Ass. pot.	? IU/ml		
Doses	(1)	(2)	
1/2.5	2.914	2.921	2.918
1/5	2.586	2.662	2.624
1/10	2.133	2.220	2.177
1/20	1.654	1.640	1.647
1/40	1.078	0.974	1.026
1/80	0.587	0.674	0.631
1/160	0.465	0.361	0.413
1/320	0.268	0.238	0.253
1/640	0.232	0.200	0.216
1/1280	0.183	0.222	0.203

**Ref. prep.:** international standard (IS), certified reference material (CRM), biological reference preparation (BRP), etc.

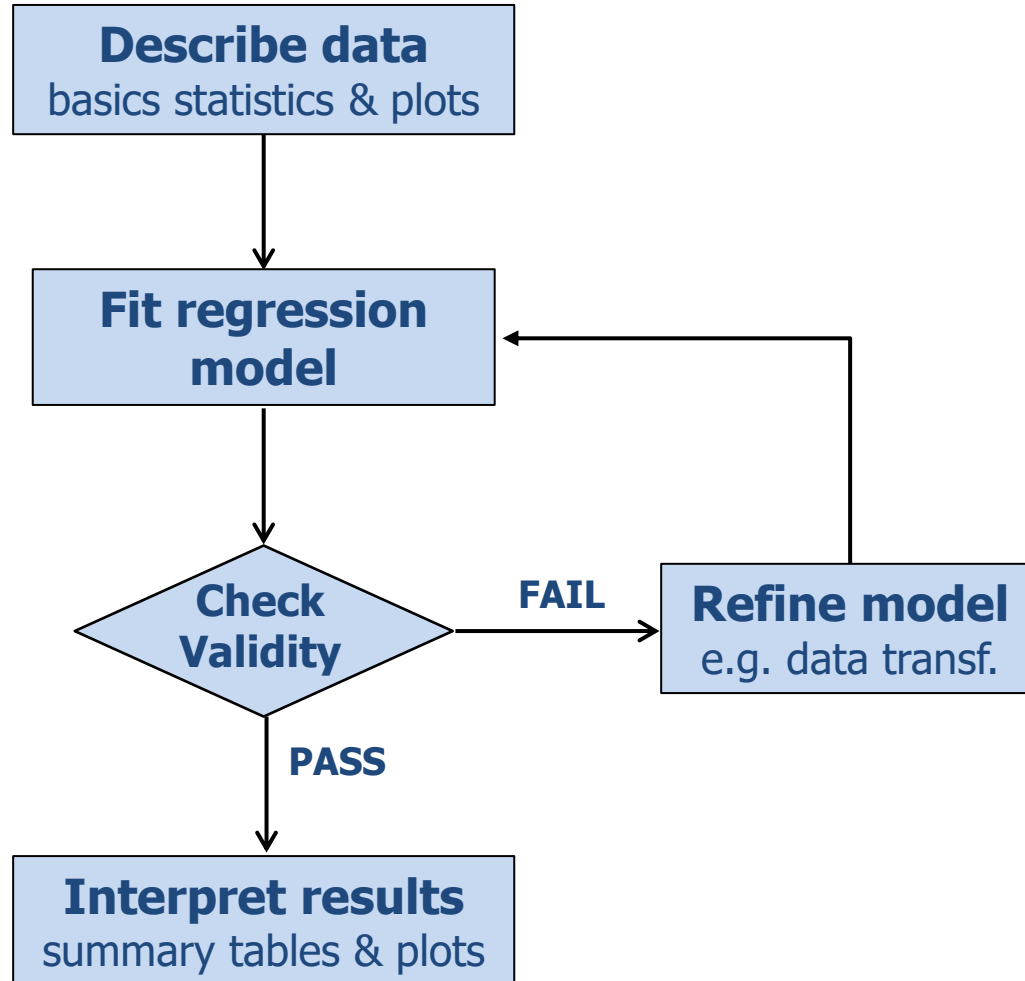
**Test prep.:** candidate IS, CRM or BRP, manufactured batches, etc.



## Test Preparation

- Relative Potency (RP)  $\sim 1/4$
- **Potency  $\sim 0.1$  IU/mL**

# Steps of statistical analysis



## Data description

### Purpose

- Check/correct any typos
- Assess data distribution (normal)
- Detect outliers, trend

### How

- Overview of raw data table
- Basic statistics (mean, std, ...)
- Scatterplot

# Data description

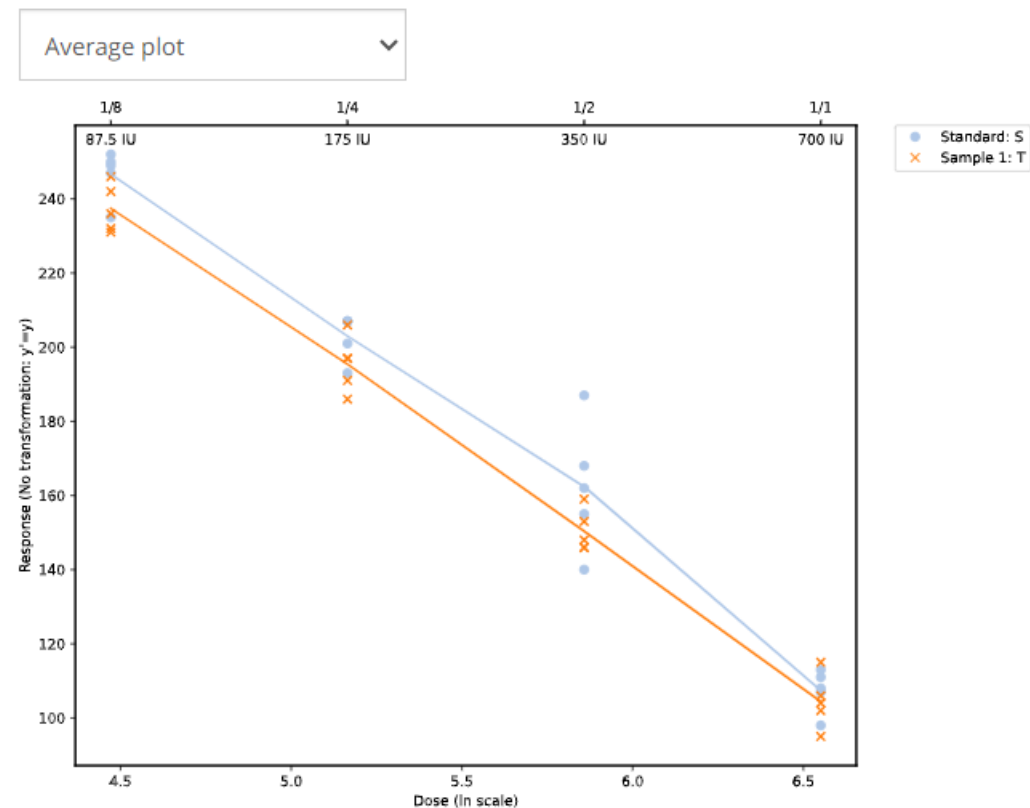
Raw data ▾ Combine

- Doses as columns
- Show statistics
- Resize all tables...

## Raw data

Table 1									
Preparation	Standard								
ID	S								
Potency	Assigned								
Potency value	700 IU/vial								
Dose	Rep.1	Rep.2	Rep.3	Rep.4	Rep.5	Mean	SD	RSD%	
1/8	252	249	247	250	235	247	7	2.7	
1/4	207	201	193	207	207	203	6	3.0	
1/2	168	187	162	155	140	162	17	10.6	
1/1	113	107	111	108	98	107	6	5.4	

Table 2									
Preparation	Sample 1								
ID	T								
Potency	Assumed								
Potency value	? IU/vial								
Dose	Rep.1	Rep.2	Rep.3	Rep.4	Rep.5	Mean	SD	RSD%	
1/8	242	236	246	231	232	237	6	2.7	
1/4	206	197	197	191	186	195	8	3.8	
1/2	146	153	148	159	146	150	6	3.7	
1/1	115	102	104	106	95	104	7	6.9	



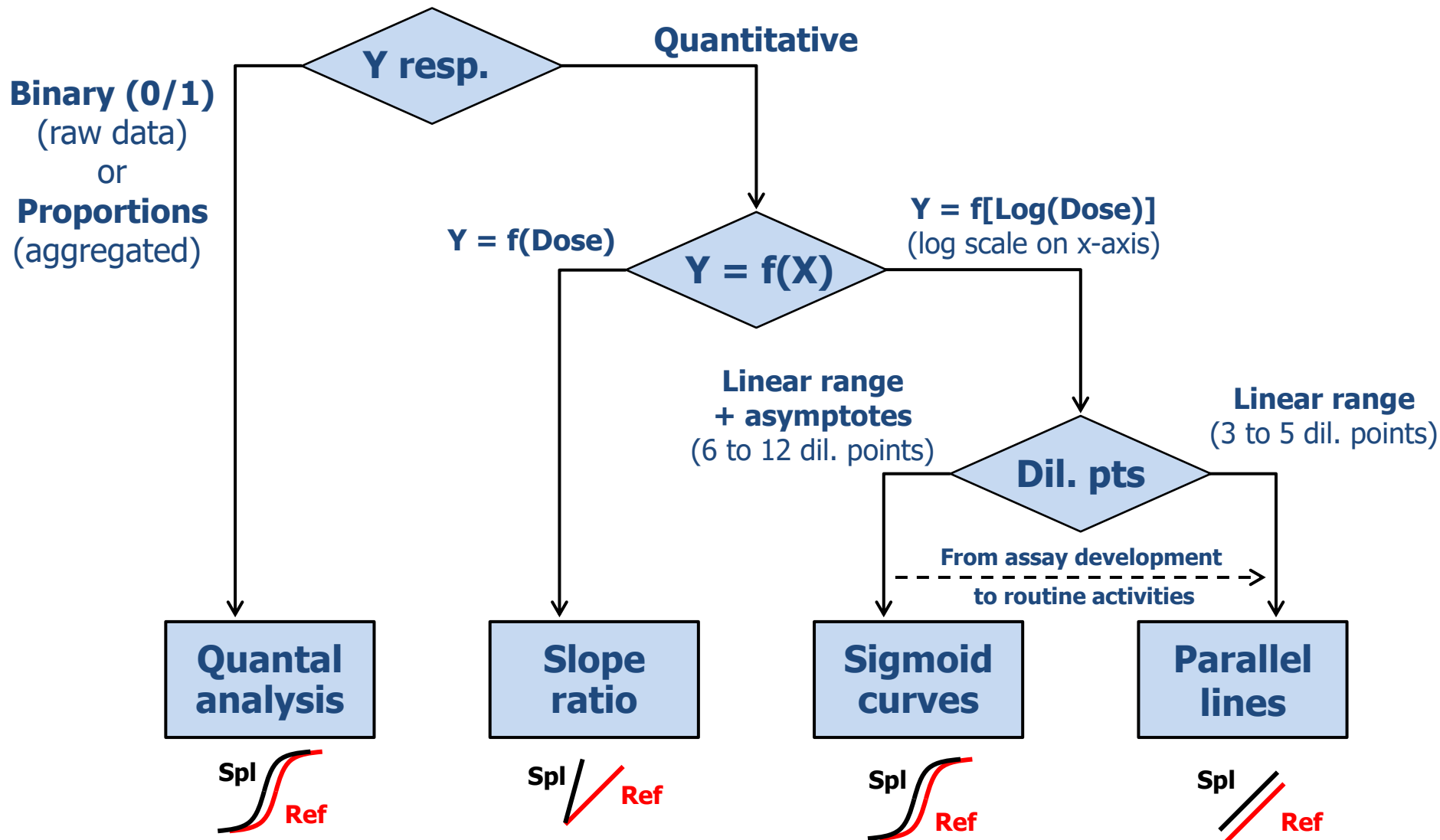
Excluded values are not displayed.

## Blank results

0.045	0.086	0.049	0.051	0.062
0.027	0.062	0.038	0.061	0.047

Mean SD RSD%  
0.053 0.016 30.5

# Regression models

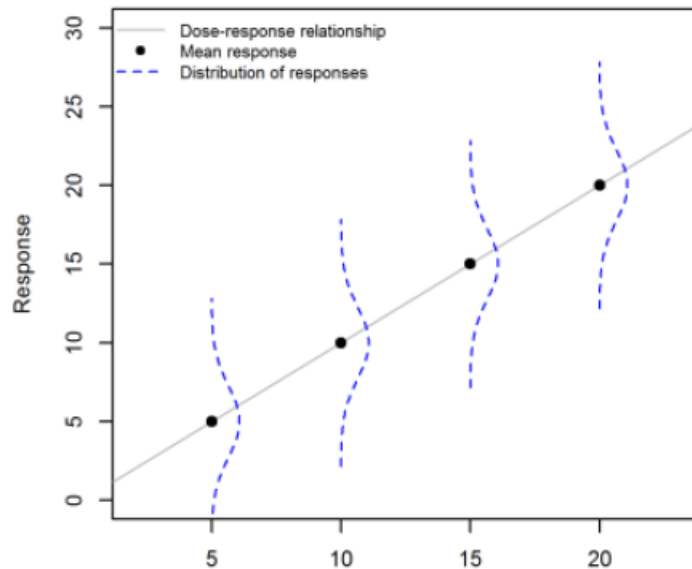




# Model validity

## PLA and SRA = linear regression lines ( $Y = a + b X + \text{error}$ )

Independent data, normally distributed with same variance across dose range

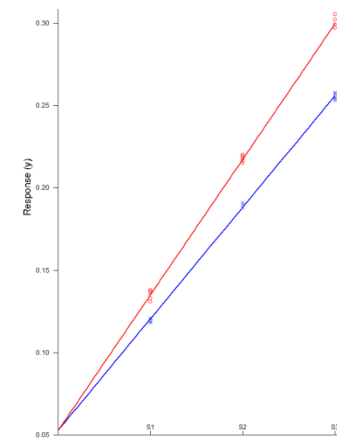
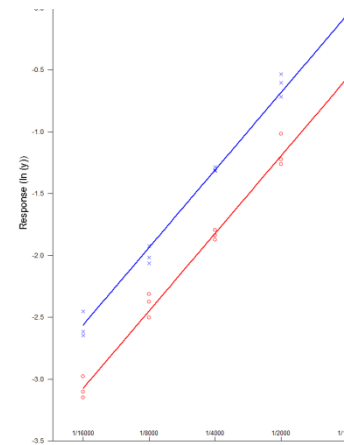


Significant regression required  
(see Anova)

**Flat slope = higher uncertainty  
about potency results**

“Good fit”: the straight line best summarises data: visual check (regression plot, residual plot) and Anova (non-linearity contrast)

- PLA: common slope => “Good parallelism” between reg. lines (visual check + Anova non-parallelism)
- SRA: common intercept (visual check + Anova intercept contrast)

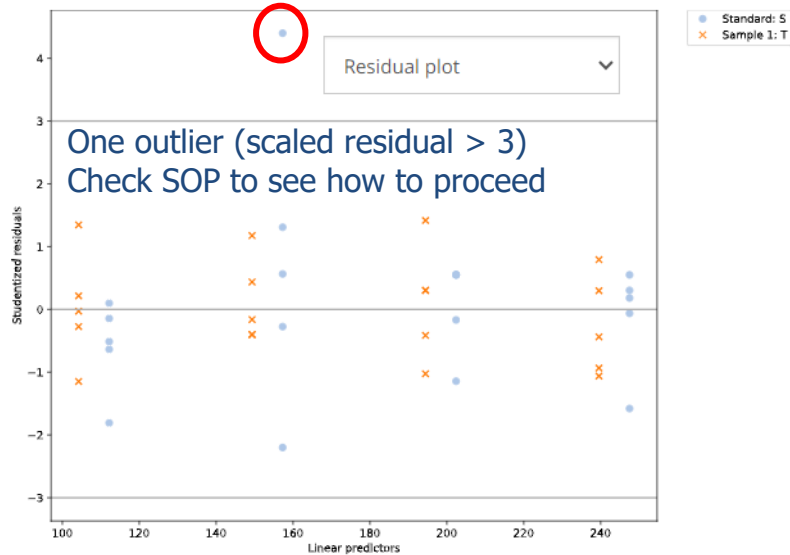
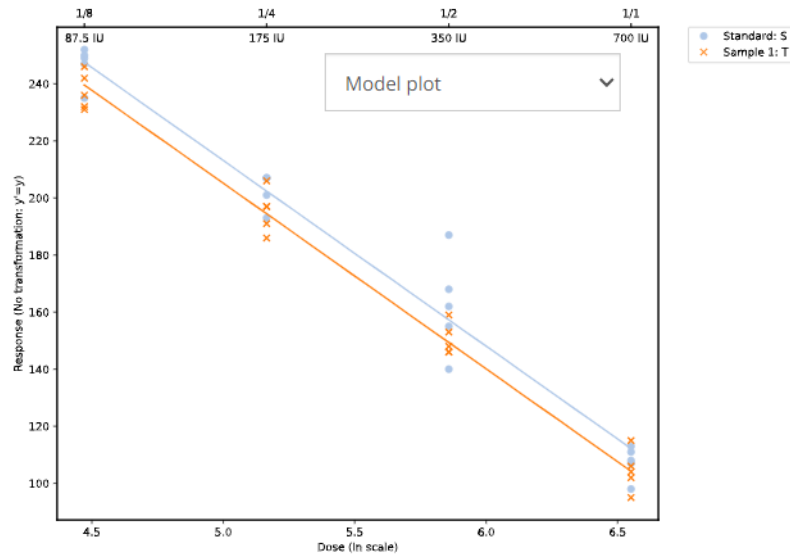


# Content

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- **Parallel-line analysis**
- Slope-ratio analysis
- 4-parameter logistic model
- 5-parameter logistic model
- 3-parameter exponential model

# Model validity, ex 1.1



## Anova table

Normal

R<sup>2</sup> All 0.974576  
R<sup>2</sup> Standard 0.965105

Source of variation	Degrees of freedom	Probability	Level of significance
Preparations	1	0.006507	**
Regression	1	< 0.000001	***
Non-parallelism	1	0.565069	
Non-linearity	4	0.493324	
Non-linearity Table 1	2	0.218293	
Non-linearity Table 2	2	0.869200	
Treatments	7	< 0.000001	***
Residual error	32		
Total	39		

Significant slope? **Yes (\*\*\*)**  
Lack of parallelism? **No (NS)**  
Lack of linearity? **No (NS)**

p-value	stars	meaning
> 0.05	no	no significant effect (NS)
≤ 0.05	*	significant effect
≤ 0.01	**	highly significant effet
≤ 0.001	***	very highly significant effet

Comparison of slopes: non-parallelism contrast (Anova) **or** equivalence testing approach (not both)

## Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	-66.1043 (-70.3250, -61.8836)	0.000000	1.00000
Sample 1: T	-64.0557 (-68.2764, -59.8349)	2.04863 (-3.92037, 8.01762)	0.969009 (0.883797, 1.06215)

Slopes: confidence limits (in brackets) calculated for a 90% confidence level (advanced options).

Differences and ratios of slopes: confidence limits (in brackets) calculated for a 90% confidence level.

	Common Slope
Estimated value	-65.0800
Lower conf. Limit	-68.0645
Upper conf. Limit	-62.0955

90% confidence level

# Model validity, ex 1.1

Advanced options

## REGRESSION TYPE

### Weighting

Robust regression (Huber's weights) ▾

Unweighted regression

Robust regression (Huber's weights)

Robust regression: in-between solution when outliers are kept in the data set

## Robust regression to alleviate the potential negative effect of the outlier

### classical regression (with outlier)

#### Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	-66.1043 (-70.3250, -61.8836)	0.000000	1.00000
Sample 1: T	-64.0557 (-68.2764, -59.8349)	2.04863 (-3.92037, 8.01762)	0.969009 (0.883797, 1.06215)

	Common Slope	
Estimated value	-65.0800	R <sup>2</sup> All 0.974576
Lower conf. Limit	-68.0645	
Upper conf. Limit	-62.0955	
		R <sup>2</sup> Standard 0.965105

### robust regression (with outlier)

#### Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	-66.4107 (-70.0356, -62.7859)	0.000000	1.00000
Sample 1: T	-64.0538 (-67.6259, -60.4817)	2.35694 (-2.73224, 7.44613)	0.964510 (0.891960, 1.04282)

	Common Slope	
Estimated value	-65.2150	R <sup>2</sup> All 0.980847
Lower conf. Limit	-67.7593	
Upper conf. Limit	-62.6707	
		R <sup>2</sup> Standard 0.976214

### classical regression (without outlier)

#### Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	-67.0270 (-70.5932, -63.4608)	0.000000	1.00000
Sample 1: T	-64.0557 (-67.6031, -60.5082)	2.97134 (-2.05881, 8.00148)	0.955670 (0.884835, 1.03193)

	Common Slope	
Estimated value	-65.5335	R <sup>2</sup> All 0.983445
Lower conf. Limit	-68.0485	
Upper conf. Limit	-63.0184	
		R <sup>2</sup> Standard 0.982764

Slopes: confidence limits (in brackets) calculated for a 90% confidence level (advanced options).

Differences and ratios of slopes: confidence limits (in brackets) calculated for a 90% confidence level.

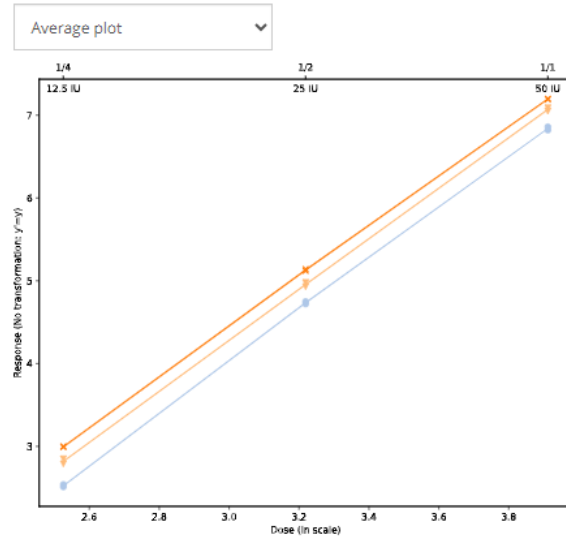
90% confidence level

# Comparison of slopes (1)

Table 1					
Preparation	Standard		Mean	SD	RSD%
Dose	Rep.1	Rep.2			
1/1	6.86	6.82	6.84	0.03	0.4
1/2	4.72	4.75	4.73	0.02	0.4
1/4	2.54	2.51	2.52	0.02	0.8

Table 2					
Preparation	Sample 1		Mean	SD	RSD%
Dose	Rep.1	Rep.2			
1/1	7.20	7.19	7.20	0.01	0.1
1/2	5.12	5.14	5.13	0.01	0.3
1/4	3.00	2.99	3.00	0.01	0.2

Table 3					
Preparation	Sample 2		Mean	SD	RSD%
Dose	Rep.1	Rep.2			
1/1	7.09	7.05	7.07	0.03	0.4
1/2	4.98	4.93	4.96	0.04	0.7
1/4	2.85	2.79	2.82	0.04	1.5



Low variability between rep. (very good repeatability) = over sensitive statistical tests (Anova) = detection of signals (non-lin, non-par) of no practical relevance...

Dose	Variances (SD <sup>2</sup> )		
	Std	Spl1	Spl2
1/1	0.00080	0.00005	0.00080
1/2	0.00045	0.00020	0.00125
1/4	0.00045	0.00005	0.00180

Pooled var. **0.00065**

Pooled SD =  $\sqrt{0.00065} = 0.0255$

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	3.11261 (3.07101, 3.15422)	0.000000	1.00000
Sample 1: T	3.02966 (2.98806, 3.07126)	-0.0829550 (-0.130632, -0.0352783)	0.973349 (0.958347, 0.988579)
Sample 2: U	3.06573 (3.02412, 3.10733)	-0.0468876 (-0.0945642, 0.000789029)	0.984936 (0.969848, 1.00026)

Slopes: confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

Differences and ratios of slopes: confidence limits (in brackets) calculated for a 90% confidence level.

Average plot > parallelism looks good

Individual slopes > ratios are indeed close to 1

Anova > however, non-parallelism is significant (\*)

What is going wrong?

Anova table

Source of variation	Mean square	F-ratio	Probability	Level of significance
Preparations	0.252117	387.872	< 0.000001	***
Regression	54.3151	561.7	< 0.000001	***
Non-parallelism	0.003325	5.11538	0.032818	*
Non-linearity	0.00181389	2.7906	0.101596	
Residual error	0.00065			
Total	3.22572			

$$\text{Stat. test} = \frac{\text{signal}}{\text{error}} = \frac{0.003325}{0.000650} = 5.11538$$

# Comparison of slopes (2)

- **Option 1:** difference testing approach  
= non-parallelism contrast (Anova table)

Anova table

Source of variation	Mean square	F-ratio	Probability	Level of significance
Preparations	0.252117	387.872	< 0.000001	***
Regression	54.3151	561.7	< 0.000001	***
Non-parallelism	0.003325	5.11538	0.032818	*
Non-linearity	0.00181389	2.7906	0.101596	
Residual error	0.00065			
Total	3.22572			

Tested against residual error, i.e. variance between replicates

Low variance (high repeatability)  
=> stat test likely to wrongly reject an assay where individual slopes are close

- **Option 2:** equivalence testing approach  
= requires **predefined** equivalence margins ( $\pm\theta$ )

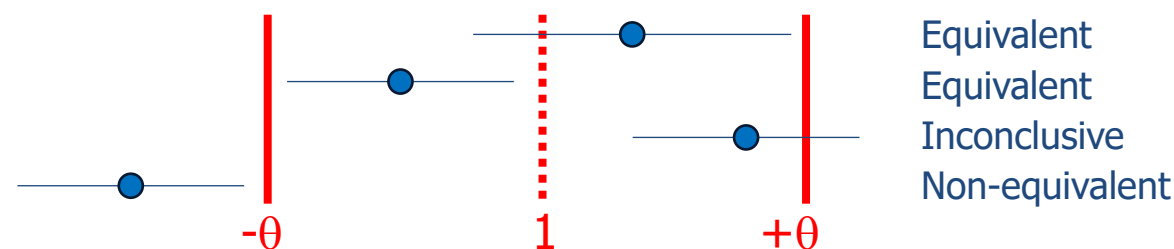
Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	3.11261 (3.07101, 3.15422)	0.000000	1.00000
Sample 1: T	3.02966 (2.98806, 3.07126)	-0.0829550 (-0.130632, -0.0352783)	0.973349 (0.958347, 0.988579)
Sample 2: U	3.06573 (3.02412, 3.10733)	-0.0468876 (-0.0945642, 0.000789029)	0.984936 (0.969848, 1.00026)

Slopes: confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

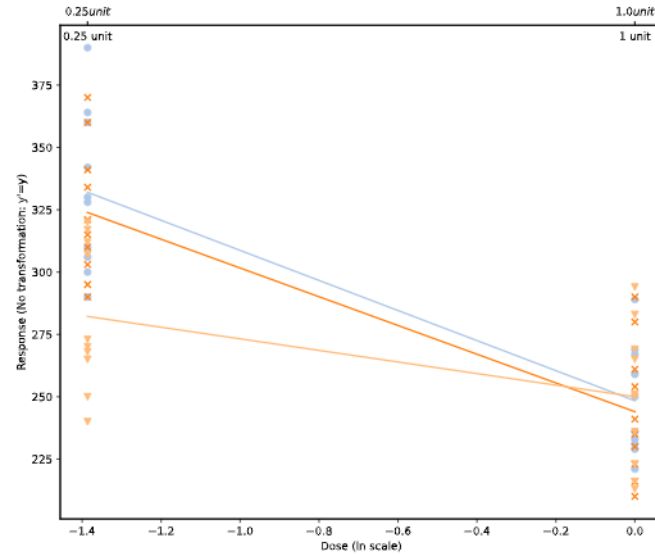
Differences and ratios of slopes: confidence limits (in brackets) calculated for a 90% confidence level.

Use differences or ratios (not both)



Use option 1 or option 2 (not both)

# Model validity, ex 3



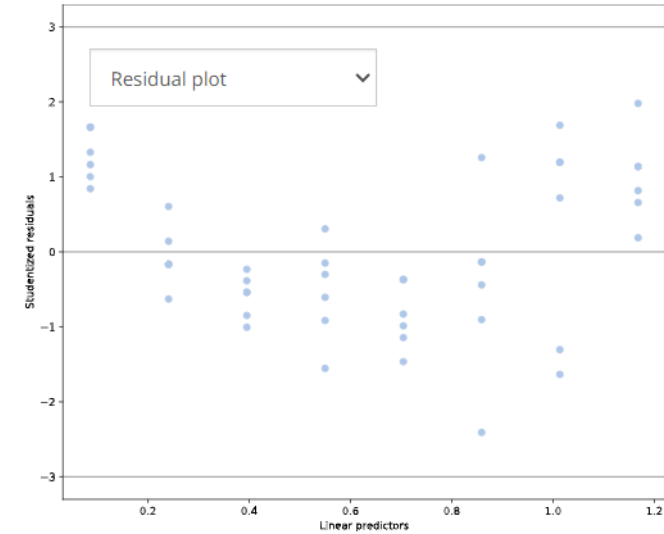
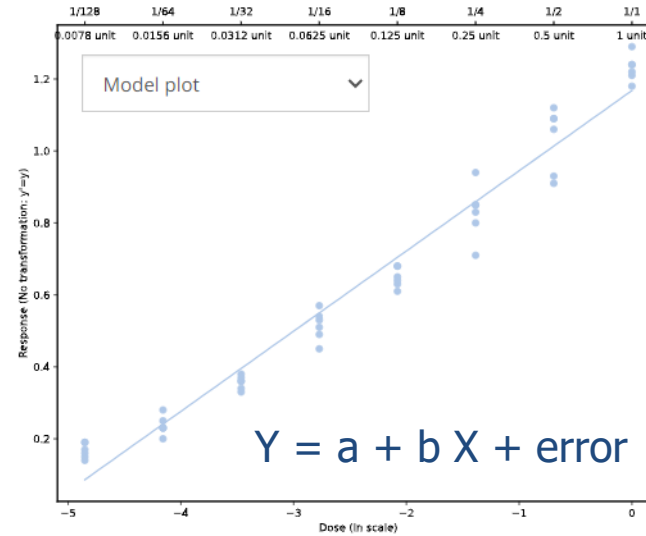
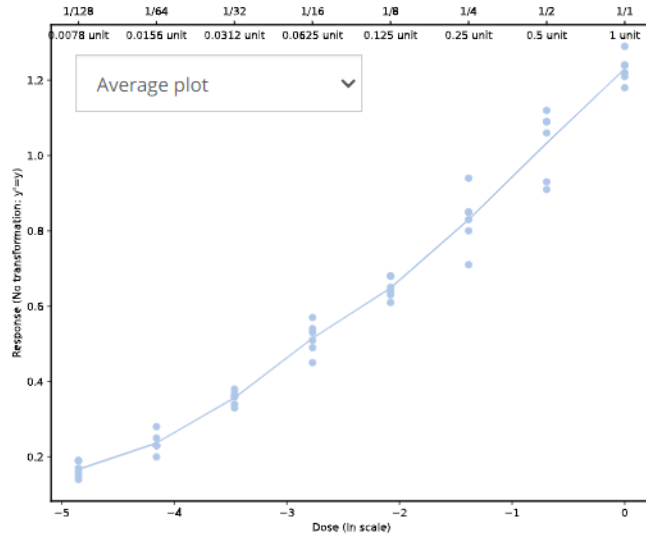
This assay is invalid... There is a lack of parallelism between the standard and one test preparation

**Two products are similar if they act as dilution of the same substance, i.e. implies parallelism on log(dose)**

Non-parallel lines may suggest problems with:

- Performance of the method, and/or
- Manufacturing process (product has changed!)

# Model validity, ex 2.1



This linear regression model is invalid... I can see it from the graphical representations

Source of variation	Degrees of freedom	Probability	Level of significance
Regression	1	< 0.000001	***
Non-linearity	6	0.000026	***
Quadratic curvature	1	< 0.000001	***
Lack of quadratic fit	5	0.840927	
Treatments	7	< 0.000001	***
Residual error	40		
Total	47		

Anova.

The slope is significant but...

Non-linearity has 3 \*\*\* Invalidity is confirmed

A quadratic term (\*\*\*) could be added:  $Y = a + b X + c X^2 + \text{error}$

Would a quadratic model be enough? Yes, lack of quadratic fit is NS

Y: measurements; a: intercept; b: slope; X: log(dose);  $X^2$ :  $[\log(\text{dose})]^2$ ; error: variability between replicates



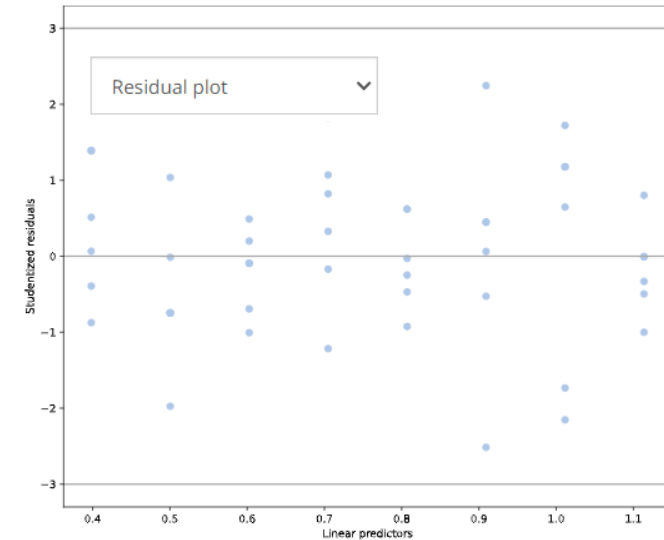
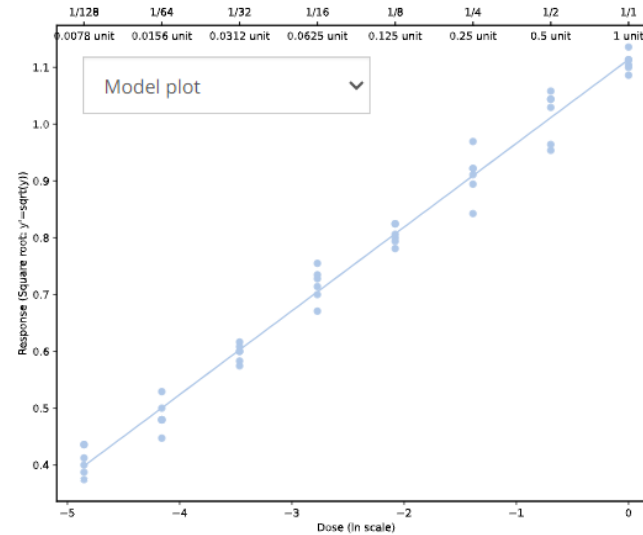
# Model validity, ex 2.2

How to improve model adequacy?

A data transformation can help

Transformation

Square root:  $y' = \sqrt{y}$



This linear regression model is valid... I can see it from the graphical representations

Source of variation	Degrees of freedom	Probability	Level of significance
Regression	1	< 0.000001	***
Non-linearity	6	0.711973	
Quadratic curvature	1	0.920982	
Lack of quadratic fit	5	0.595436	
Treatments	7	< 0.000001	***
Residual error	40		
Total	47		

Anova.

The slope is significant and...

Non-linearity is NS

Quadratic term is NS

# Potency results, ex 1

## Preparations

Table	Preparation	Information	Potency	
		ID	Potency	Value
1	Standard ▾	S	Assigned	700 IU/vial
2	Sample 1 ▾	T	Assumed ▾	800 IU/vial

} Expected value, e.g. formulation target

Potency estimates

Preparation	Units	Potency		Precise enough?		On target?	
		Estimate	(LCL, UCL)	Relative To Estimate (%)	(LCL, UCL)	Relative To Assumed/Assigned (%)	(LCL, UCL)
Sample 1: T	IU/vial	790.952	(726.139, 862.193)	100	(91.81, 109.01)	98.87	(90.77, 107.77)

Confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

### Pharm. Eur.

**Precision.** Unless otherwise stated in the monograph, the confidence limits ( $P = 0.95$ ) are not less than XX per cent and not more than YY per cent of the estimated potency.

**Recovery.** The mean recovery must not be lower than XX per cent or above YY per cent.

The amount is not less than XX per cent and not greater than YY per cent of the intended content.

# Subset analysis (SA)

## A new analysis option for PLA models

- Goal: find a subset of doses for which non-linearity and non-parallelism contrasts are NS (and the regression is significant...)
- When is it available? significant non-linearity and/or non-parallelism contrasts (all doses)

Advanced options

### SUBSET ANALYSIS

Subset

Drop

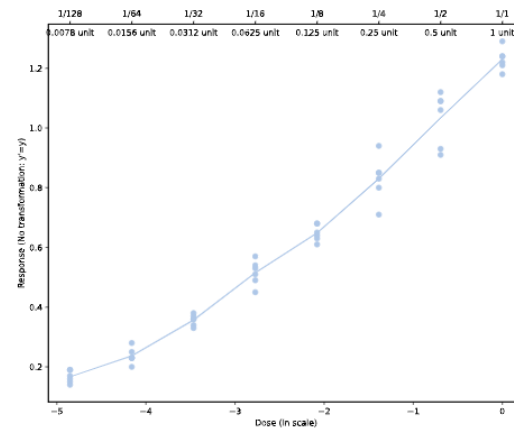
Selection criterion

Slope steepness

Slope steepness

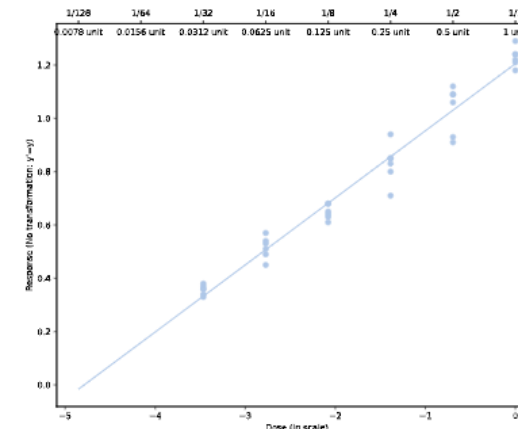
Coefficient of determination (R<sup>2</sup>)

non-linearity issue (all doses)



Subset analysis

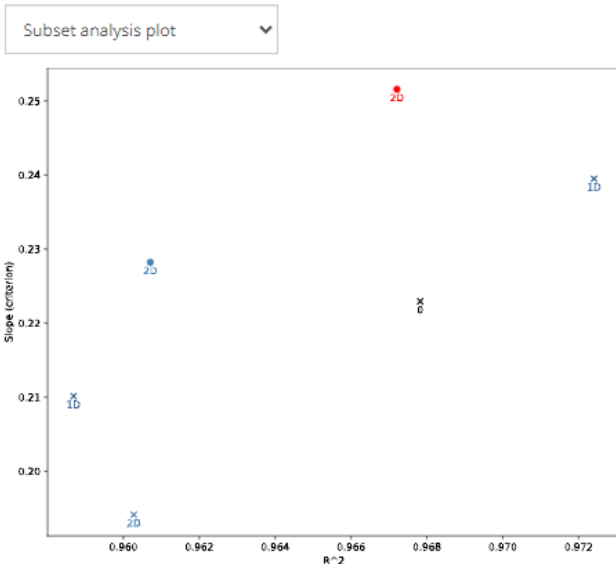
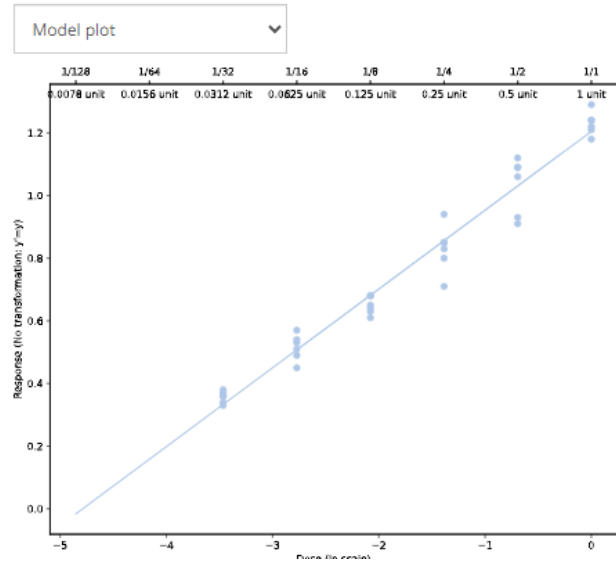
6 doses retained






Source of variation	Degrees of freedom	Probability	Level of significance
Regression	1	< 0.000001	***
Non-linearity	6	0.000026	***

Probability	Level of significance
< 0.000001	***
0.218655	

# SA > Export to Excel



Report   

Export extra analysis results to Excel

Label	Removed doses	Sequence	Probability Regression	Probability Non-linearity	Slope (criterion)	R <sup>2</sup>	Validity	Convergence	Kept
0	0	[12345678]	9.6E-38	0.000	0.223	0.968	invalid	converged	
1D	1	1 Drop: [1234567-]	7.6E-30	0.001	0.210	0.959	invalid	converged	
1D	1	1 Drop: [-2345678]	2.1E-31	0.029	0.240	0.972	invalid	converged	
2D	2	2 Drop: [123456--]	1.2E-25	0.004	0.194	0.960	invalid	converged	
2D	2	2 Drop: [-234567-]	5.3E-24	0.154	0.228	0.961	valid	converged	
2D	2	2 Drop: [--345678]	5.3E-25	0.219	0.252	0.967	valid	converged	x

Label 0: invalid regression model (all doses)

Label 1D: remove 1 dose (keep consecutive doses) => regression models remain invalid

Label 2D: remove 2 doses (keep consecutive doses) => 2 models are valid

Final model? steepest slope or highest R<sup>2</sup> (user's decision)

Label 3D? The subset analysis stopped at 2D because a valid model was found

# SA > several preparations

**SUBSET ANALYSIS**

Subset

Drop

Shift

Drop

Shift & Drop

Drop: remove the same dose number

Shift: remove a different dose number

In any case, keep contiguous doses

Case	Standard	Other prep.
1	[12345]	[12345]
-- statistical analysis, stop/continue --		
<b>Shift</b>		
2	[1234-]	[-2345]
3	[-2345]	[1234-]
-- statistical analysis, stop/continue --		
<b>Drop</b>		
4	[1234-]	[1234-]
5	[-2345]	[-2345]
-- statistical analysis, stop/continue --		
6	[123-]	[-234-]
7	[-234-]	[123-]
8	[-234-]	[-345]
9	[-345]	[-234-]
10	[123-]	[123-]
11	[-234-]	[-234-]
12	[-345]	[-345]

E.g. Shift & Drop

Label 1 (1 dose removed)

Cases 2, 3, 4, 5 will be tested

If one case is valid, then stop

Label 2 otherwise (cases 6 to 12)

...

Label k: a minimum of 3 doses

Further details in FAQ

<https://combistats.edqm.eu/faq/link/64/>

## When to use the subset analysis

- Assay development?
- Routine testing?

# Content

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- Introduction
- Parallel-line analysis
- **Slope-ratio analysis**
- 4-parameter logistic model
- 5-parameter logistic model
- 3-parameter exponential model

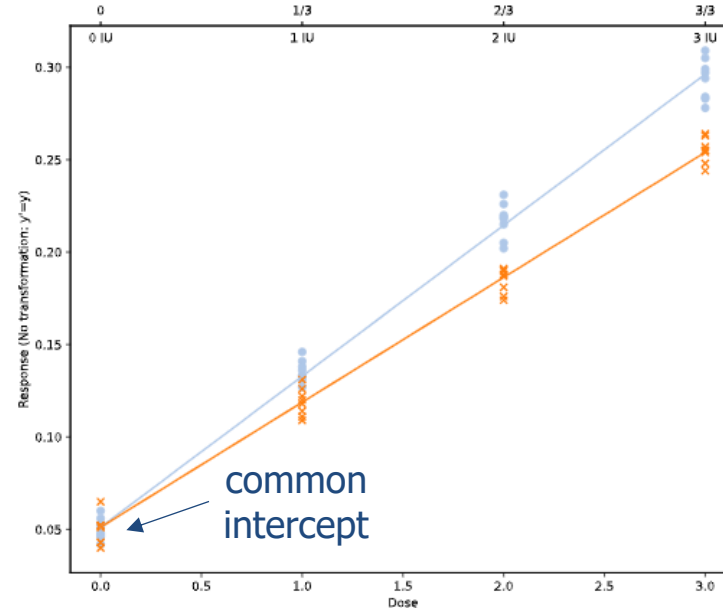
# Main differences with PLA

- x-axis: doses reported on an additive (arithmetic) scale

Table 1	
Preparation	Standard
ID	S
Potency	Assigned
Potency value	3 IU/volume
Dose	0    1/3    2/3    3/3
Rep.1	0.048    0.133    0.205    0.284
Rep.2	0.056    0.146    0.218    0.305

Doses > 0, 1, 2 and 3 IU

Zero-dose possible  
(on contrary to PLA)



Two products are similar if they act as dilution of the same substance, i.e. implies common intercepts when x-axis = doses

PLA → SRA  
Common slope (parallelism) → Common intercept (intersection)

p-value	stars	meaning
> 0.05	no	no significant effect (NS)
≤ 0.05	*	significant effect
≤ 0.01	**	highly significant effect
≤ 0.001	***	very highly significant effect

Source of variation	Degrees of freedom	Probability	Level of significance
Regression	2	< 0.000001	***
Zero-dose	1	0.307927	
Intersection	1	0.221299	
Non-linearity	2	0.620909	
Non-linearity Table 1	1	0.485277	
Non-linearity Table 2	1	0.496788	

Significant slopes? **Yes**  
(regression \*\*\*)

Common intercept ? **Yes**  
(intersection NS)

Lack of linearity? **No**  
(non-linearity NS)

# Comparison of intercepts

- **Option 1:** difference testing approach  
= intersection contrast in Anova table

Source of variation	Degrees of freedom	Probability	Level of significance
Regression	2	< 0.000001	***
Zero-dose	1	0.307927	
Intersection	1	0.221299	
Non-linearity	2	0.620909	
Non-linearity Table 1	1	0.485277	
Non-linearity Table 2	1	0.496788	
Treatments	6	< 0.000001	***
Residual error	57		

Tested against residual error, i.e. variance between replicates.

Low variance (high repeatability) => stat test likely to wrongly reject an assay where intercepts are quite close

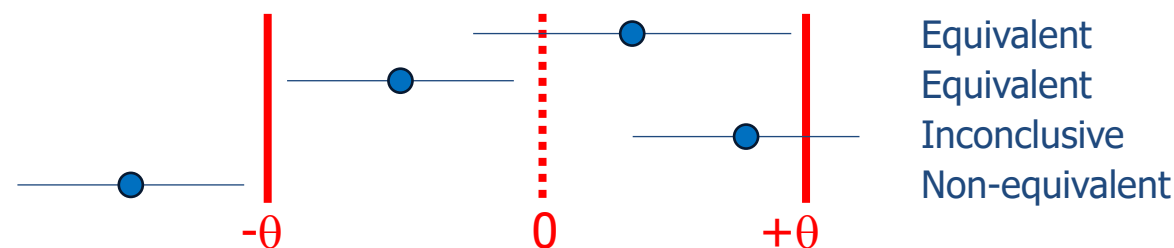
- **Option 2:** equivalence testing approach  
= requires **predefined** equivalence margins ( $\pm\theta$ )

## Equivalence of intercepts

Preparation	Intercept	Difference with Standard
Standard: S	0.0574167 (0.0503656, 0.0644677)	0.000000
Sample 1: T	0.0500417 (0.0429906, 0.0570927)	-0.00737500 (-0.0173467, 0.00259671)

Intercepts: confidence limits (in brackets) calculated for a 90% confidence level (advanced options).

Differences of intercepts: confidence limits (in brackets) calculated for a 90% confidence level.



Use option 1 or option 2 (not both)

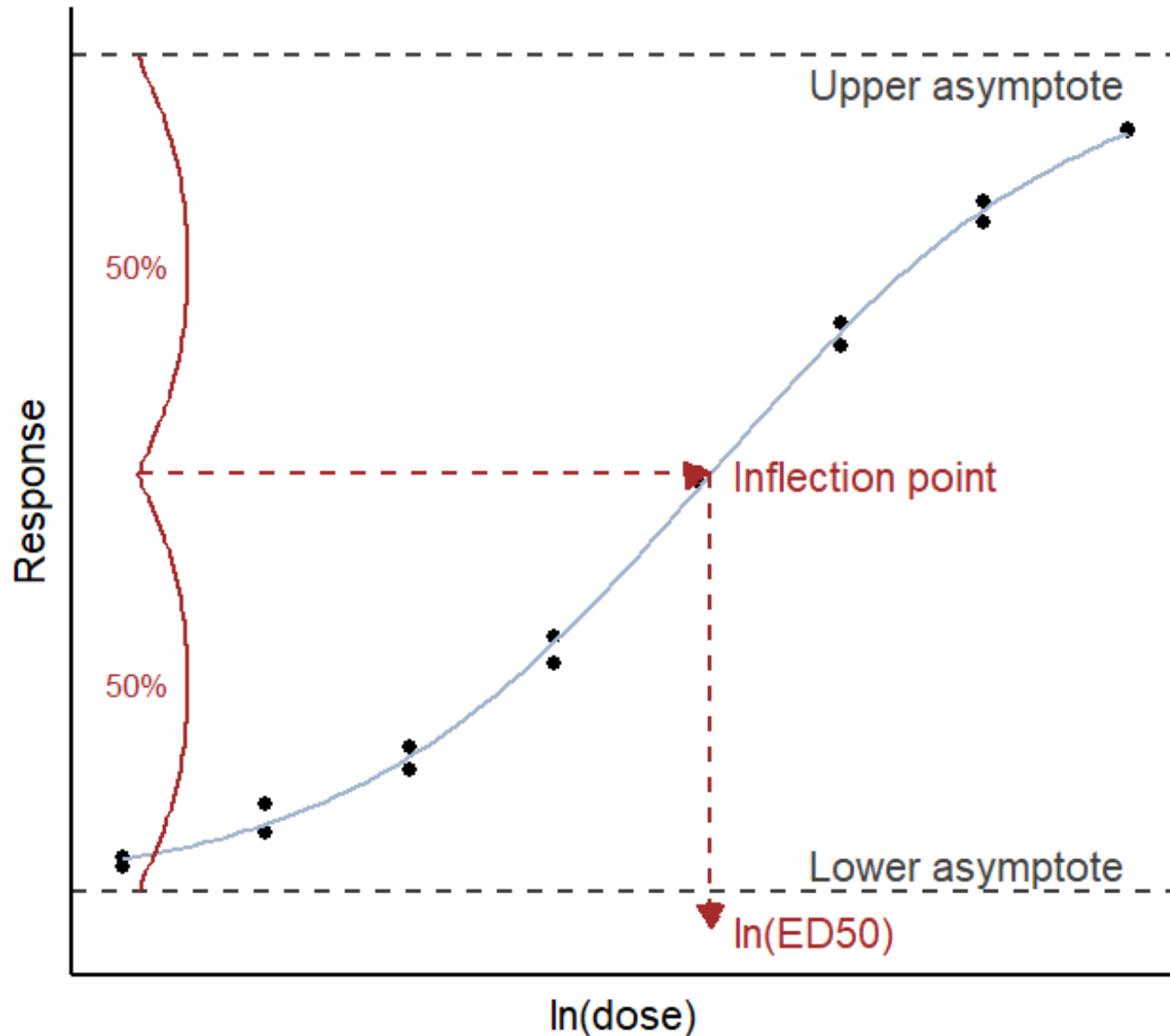


# Content

---

- Introduction
- Parallel-line analysis
- Slope-ratio analysis
- **4-parameter logistic model**
- 5-parameter logistic model
- 3-parameter exponential model

# 4PL – dose-response relationship



## Symmetrical S-shaped curve

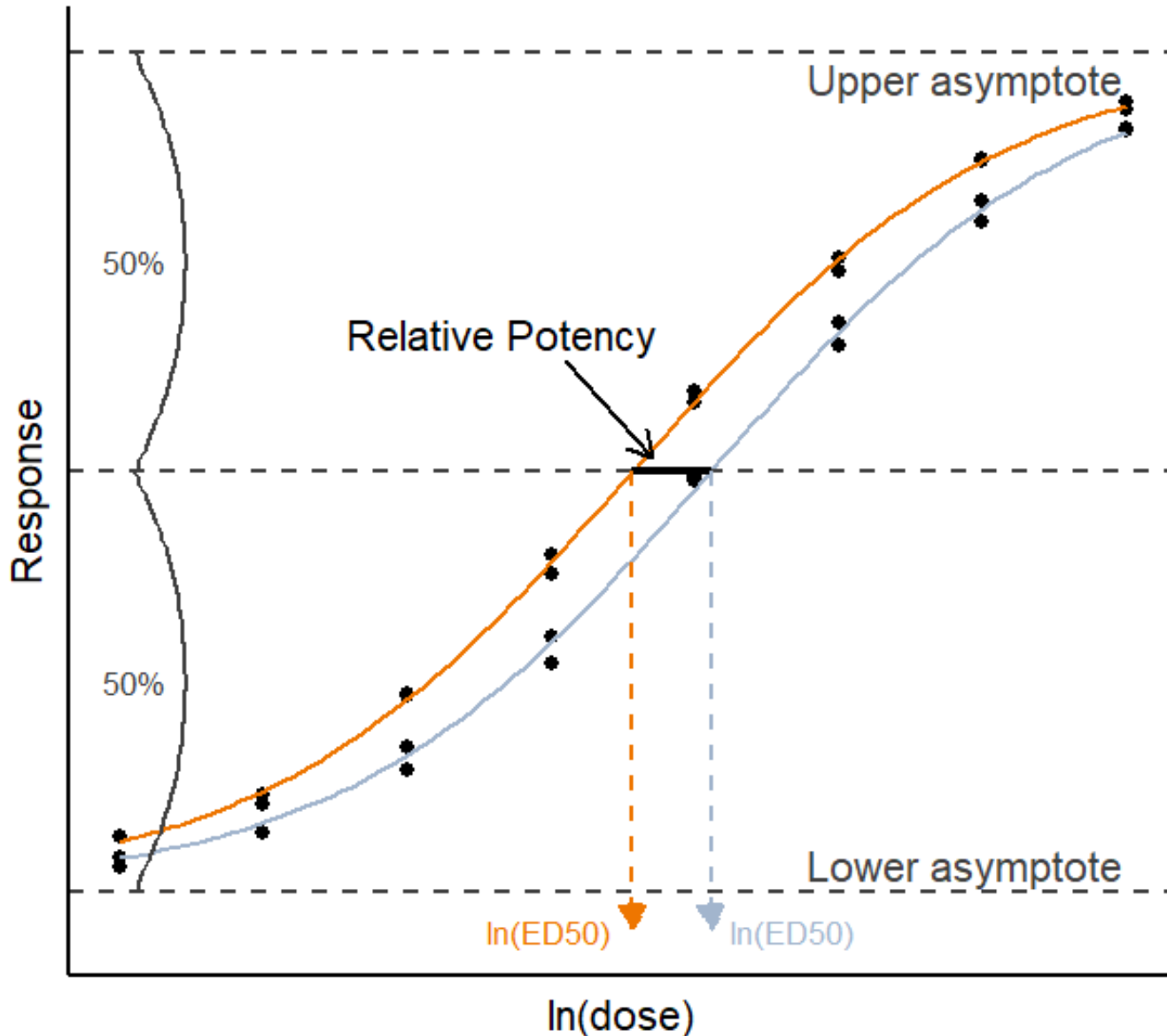
- One to two concentrations for each asymptotes
- Three to four concentrations for linear part of the curve

$$Response = D + \frac{A - D}{1 + \exp(B * (\ln(dose) - C))}$$

where *D*: lower asymptote  
*A*: upper asymptote  
*C*: inflection point (=ED50)  
*B*: slope parameter

Assays: ELISA or cell-based potency assays

# 4PL - Potency



## Assumptions

**Reference** and **Test** have the same biological activity

- Common slope, lower and upper asymptotes are the same (*constrained model*)

*Visual verification*

- Similar behaviour across the whole range of doses

*Check assay validity criteria*

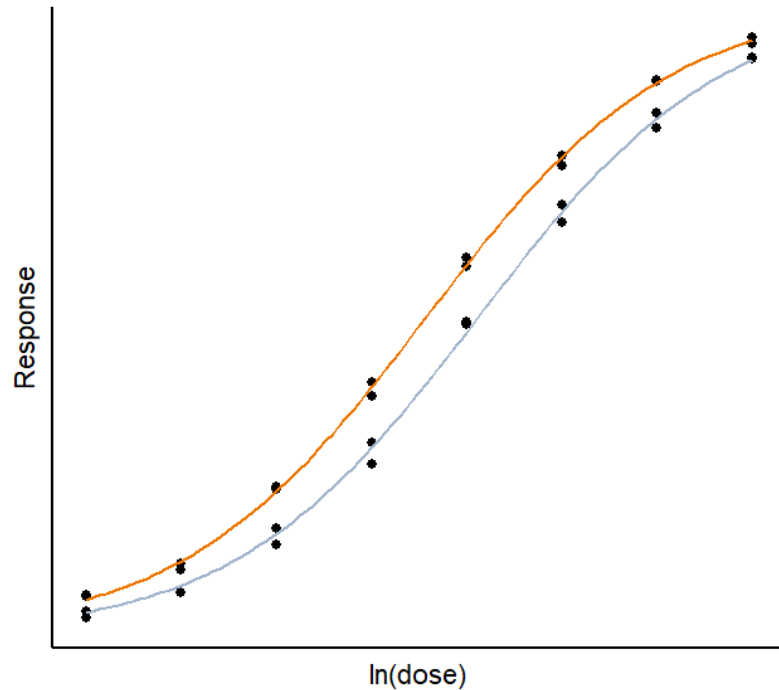
- Variability of response data is the same for each dose and follows normal distribution

*Check residual plot*

## Relative Potency

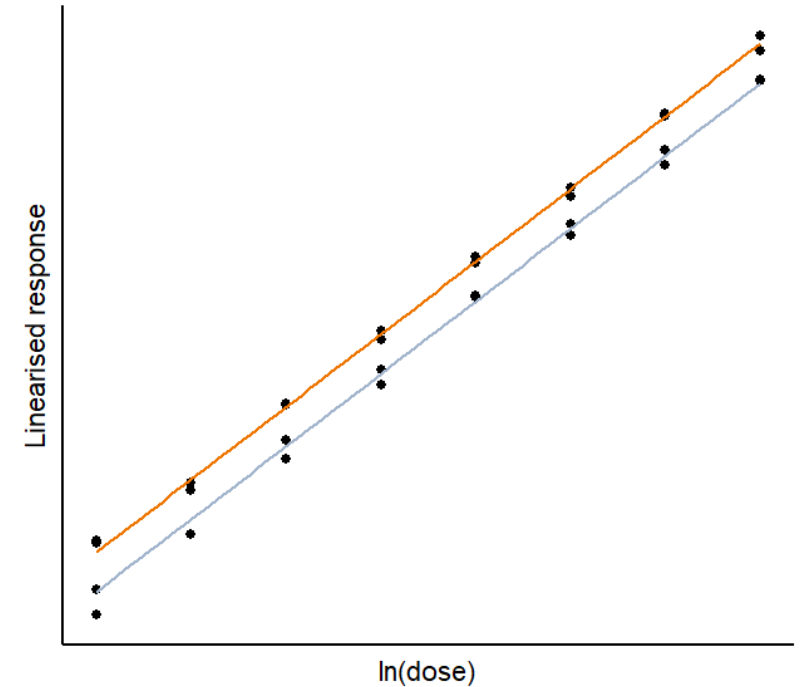
largest distance between preparations

# 4PL – Assay validity criteria



Linearisation of dose-response relationship via logit transformation (default)

Analysis of variance (ANOVA) performed on linearised data to access assay validity



## Validity criteria

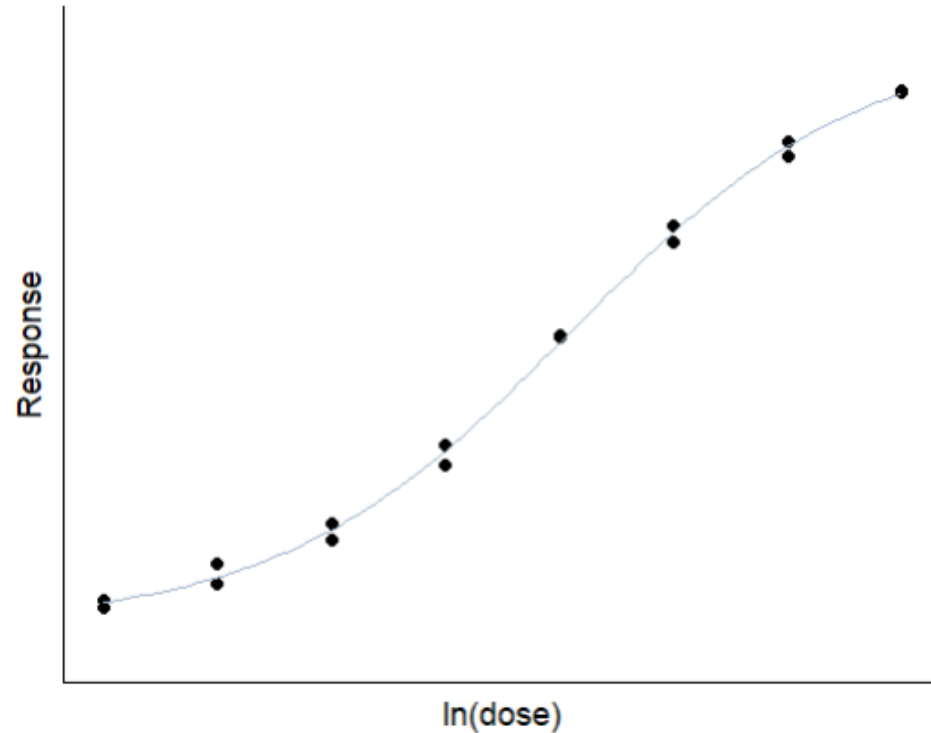
- The p-value for **regression** is significant
- The p-value for **non-parallelism** is not significant
- The p-value for **non-linearity** is not significant

Source of variation	Probability	Level of significance
Preparations	0.328776	
Regression	< 0.000001	***
Non-parallelism	0.696804	
Non-linearity	0.937394	

# 4PL assumption: constant variability at each dose

## Assumption

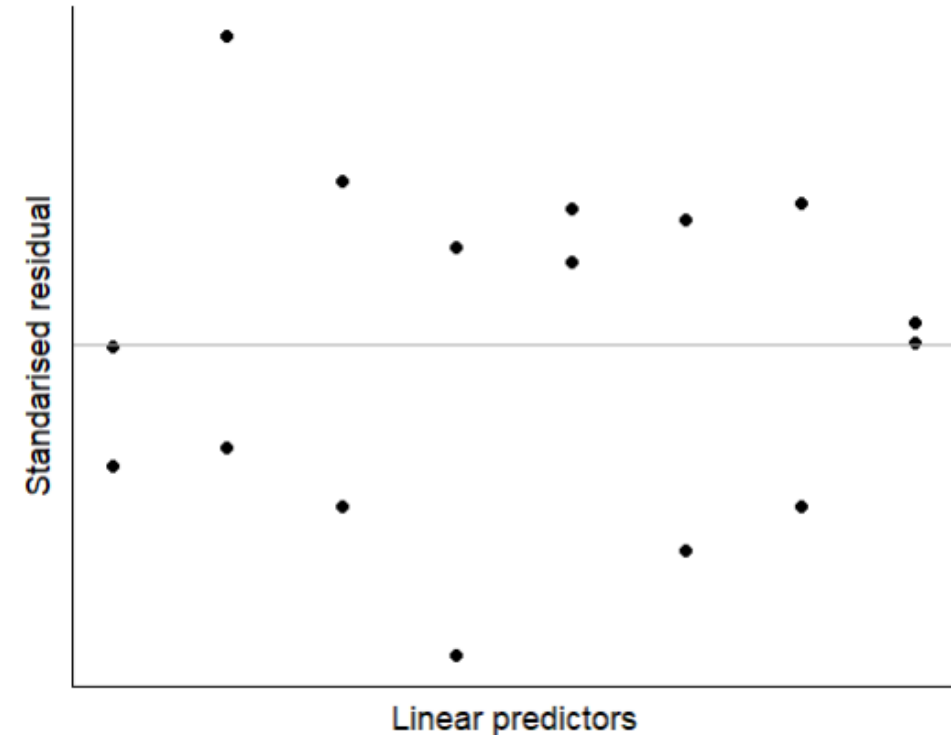
Variability of response data is the **same for each dose** and follows **normal distribution**



## Verification

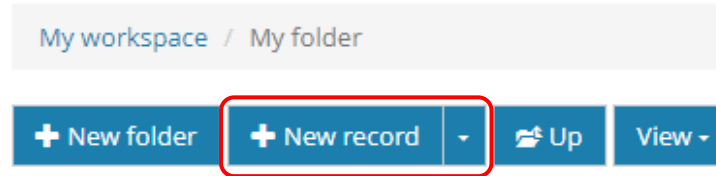
**Similar variability over doses:** inspect residual plot *same dispersion of the points around the vertical line*

**Normal distribution** not enough data to evaluate



# 4PL – create a record

## 1. Create a new record



## Taskbar in editor



## 2. Enter the record name, select destination folder and set-up

### New record

#### Type

Assay

#### Name

Assay1\_4PL

#### To folder

David

Elena

My folder

#### Assay

Multiple-dose

#### Type of design

Completely randomised

#### Response variable

Quantitative

#### Model

Sigmoid curves (4-PL, In dose)

#### Preparations

2

#### Max doses

5

#### Max replicates

3

Cancel

Create

# 4PL – data entry

## Preparations

Table	Preparation	Information		Potency		Pre-dilution	
		ID	Long label	Potency	Value	Reconstitution	Stock solution
1	Standard ▾	S	standard	Assigned	100 IU/amp.	1 amp./mL	1 mL/10 mL
2	Sample 1 ▾	T	test sample	Assumed ▾	80 IU/vial	1 vial/0.5 mL	0.5 mL/5 mL
3	Sample 2 ▾	C1	Control 1	Assumed ▾	25 IU/mL		
4	Sample 3 ▾	C2	Control 2	Assumed ▾	120 IU/mL		

Observ.	c1	c2	c3	c4	c5	c6	c7	c8	c9	c10	c11	c12
r1												
r2	0.031	0.044	0.027	0.032	0.028	0.051	0.117	0.097	0.104	0.093	0.112	0.047
r3	0.046	2.912	2.579	2.130	1.651	1.073	0.585	0.463	0.266	0.228	0.176	0.031
r4	0.024	2.917	2.654	2.212	1.638	0.973	0.666	0.356	0.234	0.197	0.215	0.050
r5	0.030	3.017	2.801	2.401	1.918	1.364	0.861	0.497	0.340	0.242	0.178	0.035
r6	0.045	2.987	2.808	2.450	1.963	1.299	0.854	0.496	0.344	0.217	0.125	0.024
r7	0.051	2.105	2.074	2.162	1.948	2.037	1.974	1.925	2.017	2.106	1.938	0.038
r8												

## Blank results

0.031	0.046	0.024	0.030	0.045	0.051
0.047	0.031	0.050	0.035	0.024	0.038

*Mean*   *SD*   *RSD%*  
0.038   0.010   26.2

<https://combistats.edqm.eu/help/>

Table 1					
Preparation	Standard				
ID	S				
Long label	standard				
Potency	Assigned				
Potency value	100 IU/amp.				
Reconstitution	1 amp./mL				
Stock solution	1 mL/10 mL				
Dose	Rep.1	Rep.2	Mean	SD	RSD%
1/1	2.912	2.917	2.914	0.004	0.1
1/2	2.579	2.654	2.617	0.053	2.0
1/4	2.130	2.212	2.171	0.058	2.7
1/8	1.651	1.638	1.644	0.009	0.6
1/16	1.073	0.973	1.023	0.071	6.9
1/32	0.585	0.666	0.626	0.057	9.2
1/64	0.463	0.356	0.410	0.076	18.5
1/128	0.266	0.234	0.250	0.023	9.1
1/256	0.228	0.197	0.213	0.022	10.3
1/512	0.176	0.215	0.196	0.028	14.1

EN01 Information And Remarks  
 EN02 Taskbar  
 EN05 Preparations Table  
 EN06 Rawdata Tables  
 EN07 Show Design  
 EN08 Table of Blank Results

## Wizard

### Assay

Multiple-dose

### Type of design

Completely randomised

### Response variable

Quantitative

### Model

Sigmoid curves (4-PL, In dose)

### Transformation

No transformation:  $y'=y$

### Linearising transformation

Logit

### Variance

Observed residuals

### Transformation

No transformation:  $y'=y$

No transformation:  $y'=y$

Inverse:  $y'=1/y$

Logarithm:  $y'=\log(y)$

Square root:  $y'=\sqrt{y}$

Square:  $y'=y^2$

User-defined:  $y'=...$

### Variance

Observed residuals

Observed residuals

Deviation from linearity

Deviation from model

User-defined ( $s^2$ )

Responses can be transformed prior applying linearising transformation

### Linearising transformation

Logit

Probit

Logit

Angular

Rectangular

Gompit

If observed residuals cannot be calculated or are not representative other options are available

## Advanced options

### FIXED PARAMETER

Slope

1.0

Addition

0.15

Multiplication

3.3

3 model parameters can be fixed:

Addition = lower asymptote   
Multiplication = upper – lower asymptote

### CONFIDENCE LEVELS

Slope / intercept

95 %

Potency / Effective dose / Inverse prediction

95 %



Slope/intercept  
New record: 95%  
Imported from Desktop: 90%

### REGRESSION TYPE

Weighting

Unweighted regression

Unweighted regression

Weighted regression (1/m<sup>2</sup>)

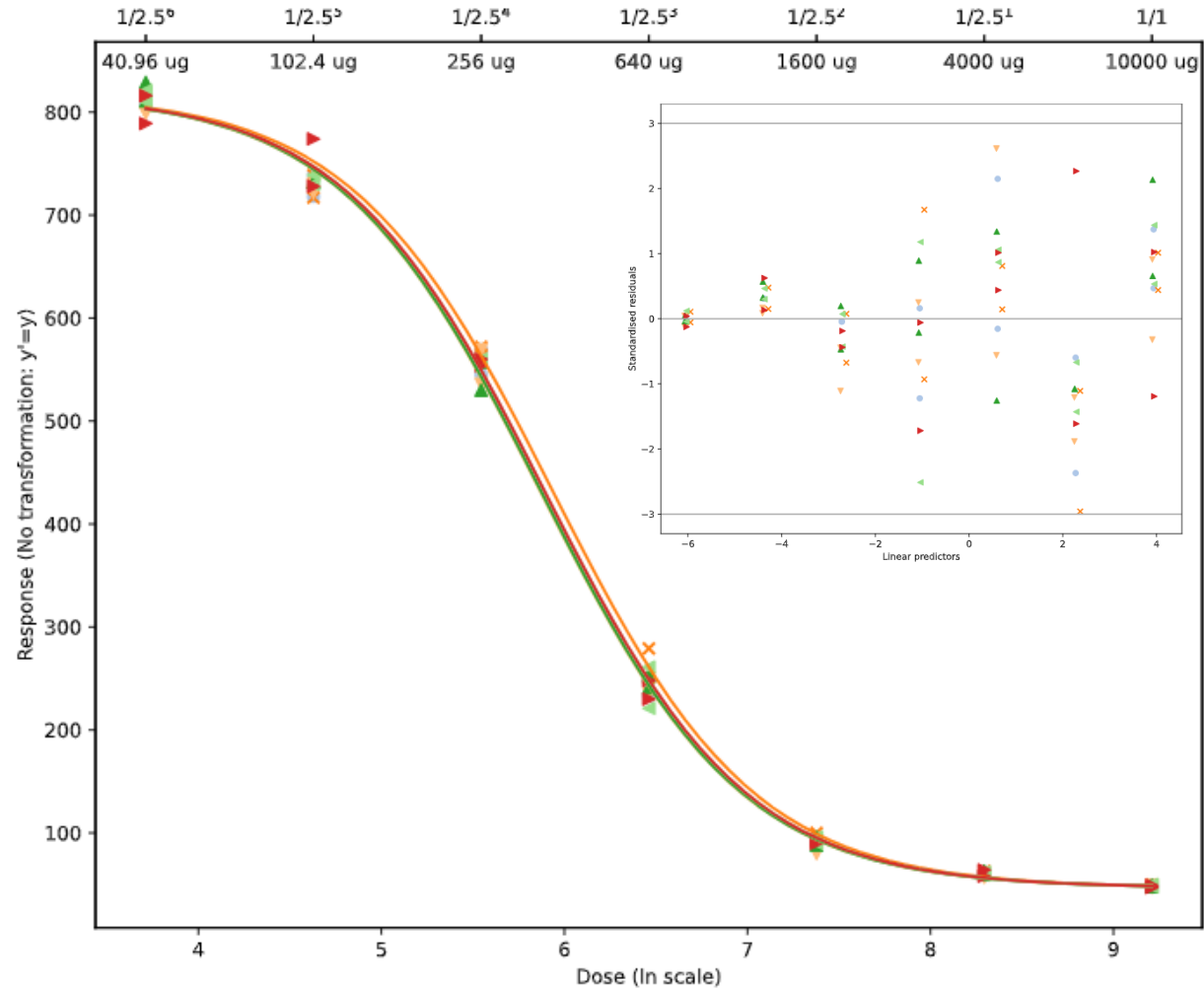
User-defined (w=...)

Weighting regression may help to stabilise the residuals over the range of responses.

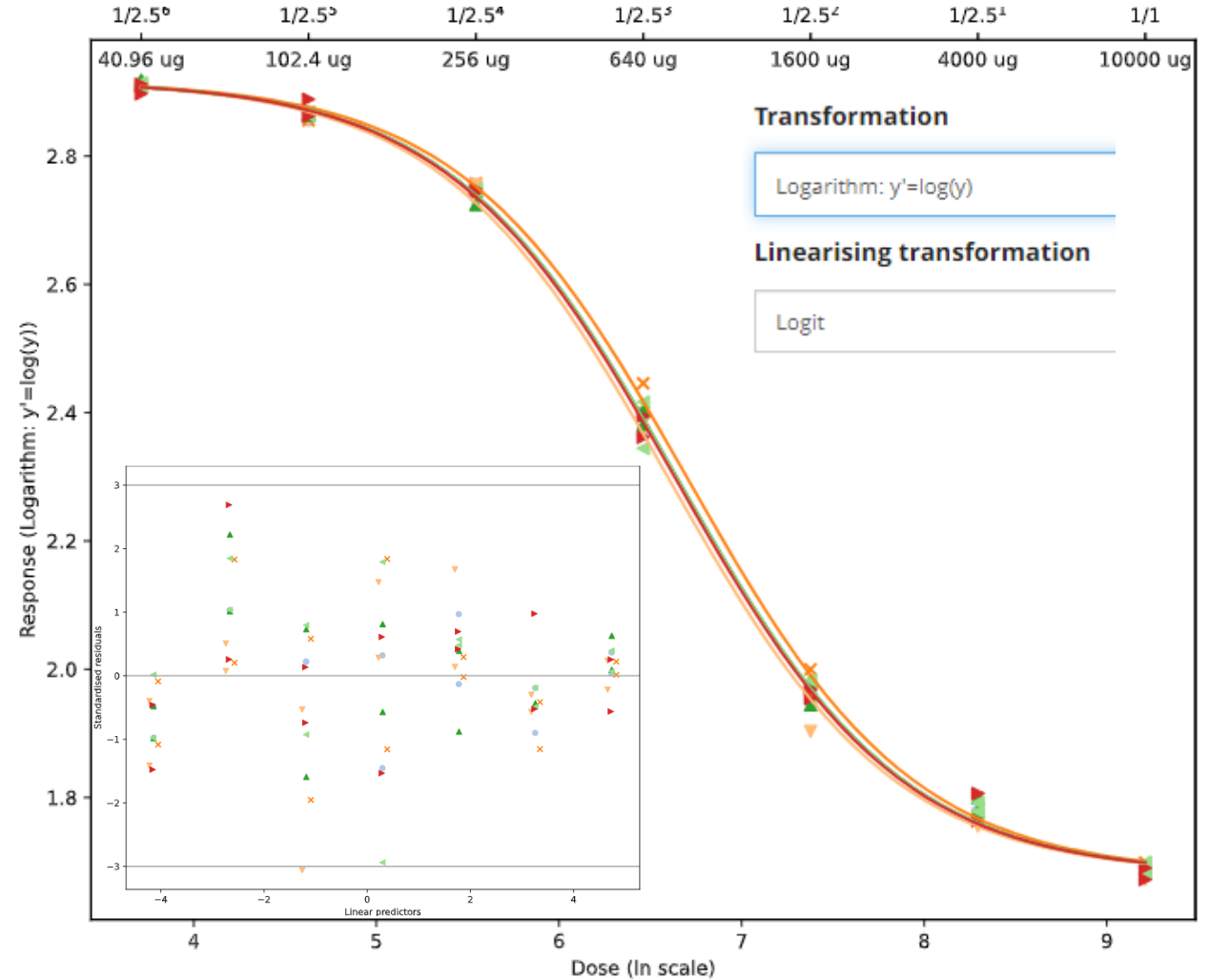


# 4PL example: log + logit transformation

Variability is higher at higher response



4PL on log-transformed responses



# Linearising transformations

## Linearising transformation

Logit

Probit

Logit

Angular

Rectangular

Gompit

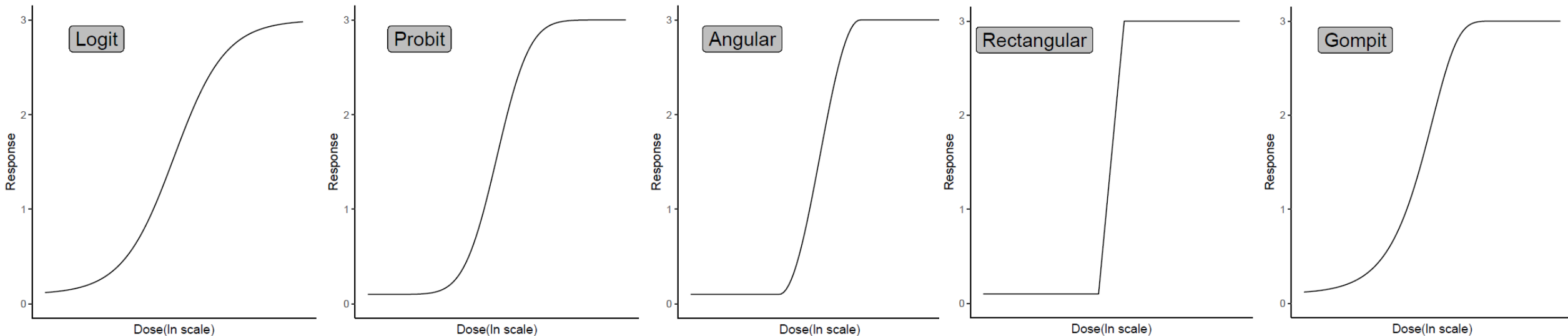
**Logit:** symmetrical with long tails (default for quantitative response)

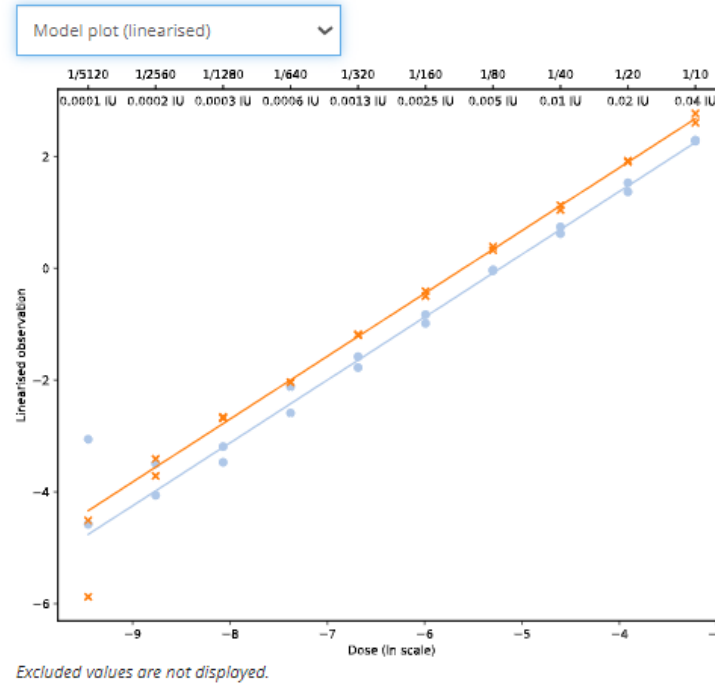
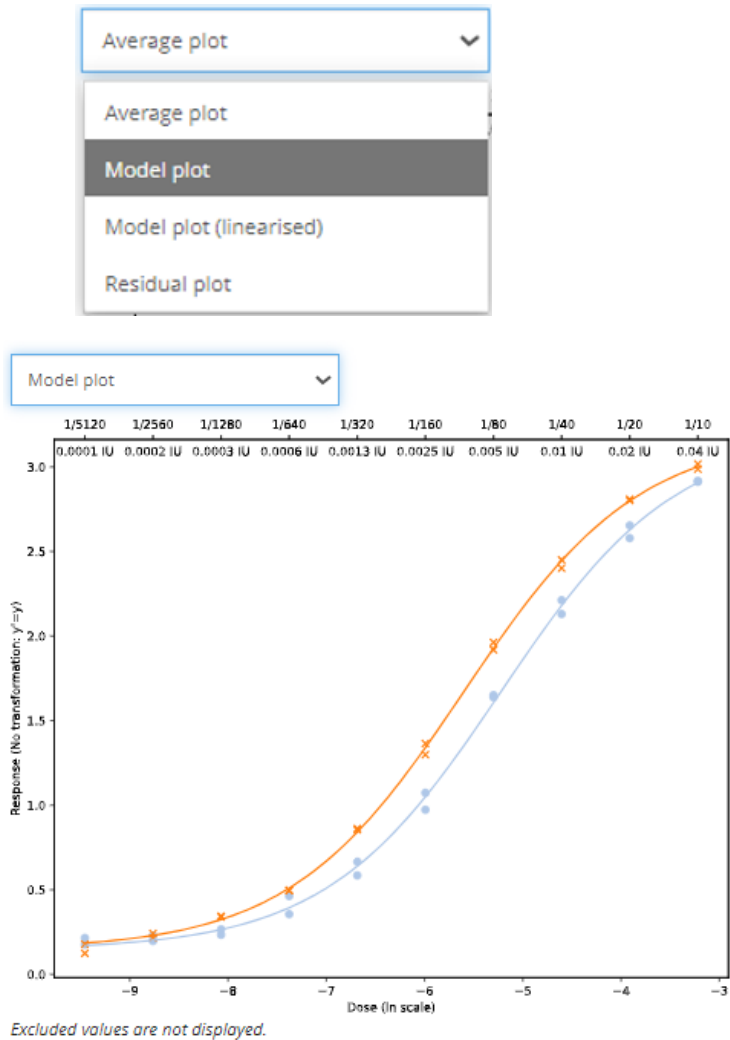
**Probit:** symmetrical with short tails

**Angular:** symmetrical without tails

**Rectangular:** shaped like straight lines (not used anymore)

**Gompit:** asymmetrical with one long tail and one short tail

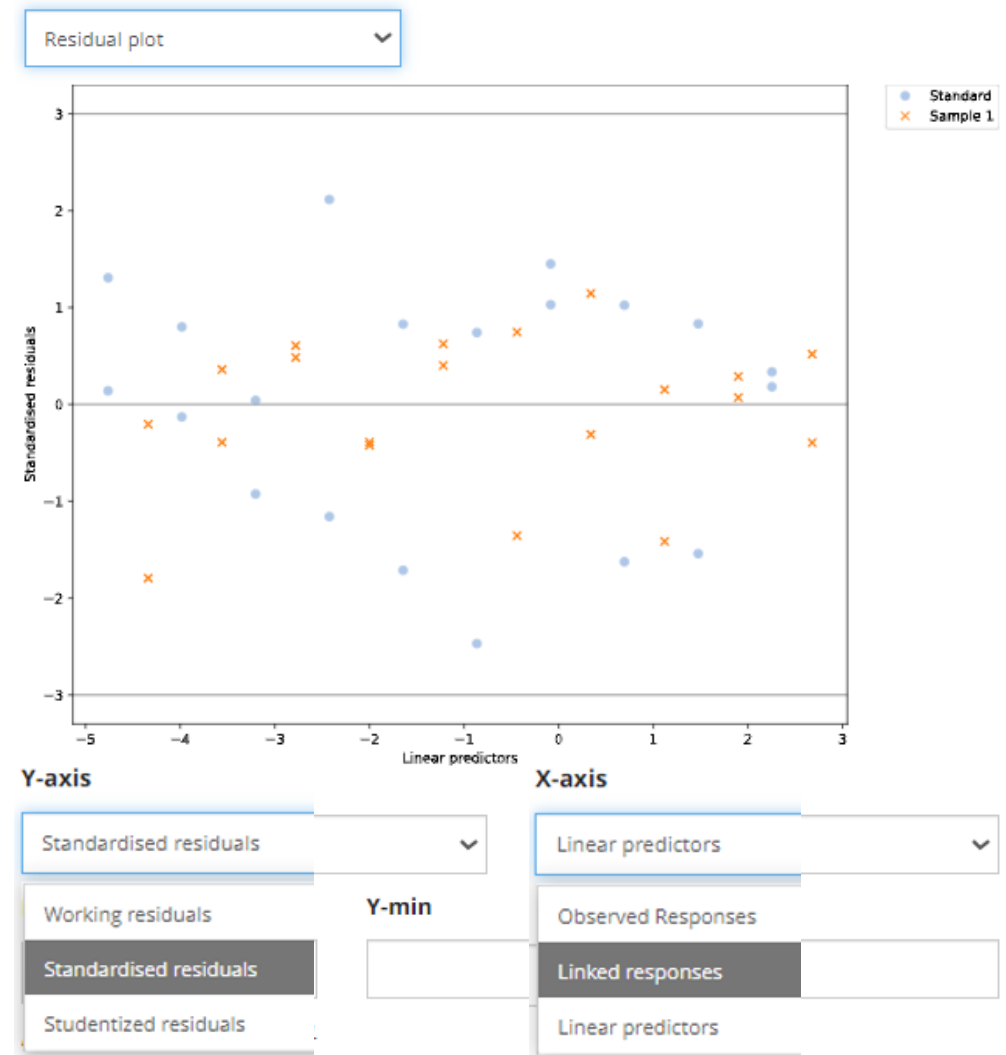




Model plot (linearised) useful if non-linearity or non-parallelism criteria not met

Residual plot useful to check

- variability over the dose range
- outliers



# 4PL - Summary statistics

## Regression parameters

Global model: convergence reached

R<sup>2</sup> Standard: convergence reached

	weighted	unweighted
R <sup>2</sup> All	0.991457	0.998112
R <sup>2</sup> Standard	0.993511	0.998558

EN10 Regression Parameters

EN11 ANOVA Table

EN12 Equivalence of Slope

### Common Slope

Estimated value	1.12452
Lower conf. Limit	1.08725
Upper conf. Limit	1.16179

### Other model parameters

Lower asymptote	0.145458
Upper asymptote	3.19599

95% confidence level

## Anova table

Normal ▼

Source of variation	Degrees of freedom	Sum of squares	Mean square	Chi-square	Probability	Level of significance
Preparations	3	0.813672	0.271224	301.79	< 0.000001	***
Regression	1	9.43054	9.43054	3497.77	< 0.000001	***
Non-parallelism	1	6.55525e-05	6.55525e-05	0.0243133	0.876090	
Non-linearity	16	0.0127084	0.000794275	4.71353	0.997004	
Non-linearity Table 1	8	0.00764179	0.000955224	2.83433	0.944320	
Non-linearity Table 2	8	0.00506661	0.000633326	1.8792	0.984494	
Treatments	21	10.257	0.488428	3804.3	< 0.000001	***
Residual error	28	0.0754923	0.00269615			
Total	49	10.3325	0.210867			

## Equivalence of slopes

Preparation	Slope	Difference with Standard	Ratio with Standard
Standard: S	1.12755 (1.07426, 1.18084)	0.000000	1.00000
Sample 1: T	1.12162 (1.06949, 1.17375)	-0.00593102 (-0.0684964, 0.0566344)	0.994740 (0.940903, 1.05171)

Slopes: confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

Differences and ratios of slopes: confidence limits (in brackets) calculated for a 90% confidence level.

# 4PL - Potency and effective dose values

EN15 Potency Estimates  
EN16 Effective Dose & Prediction

## Potency estimates

Precision Recovery

Preparation	Units	Potency		Relative To Estimate (%)		Relative To Assumed/Assigned (%)	
		Estimate	(LCL, UCL)	Rel. To Est.	(LCL, UCL)	Rel. To Ass.	(LCL, UCL)
Sample 1	IU/ml	0.583544	(0.556798, 0.611586)	100	(95.42, 104.81)	145.89	(139.20, 152.90)

Confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

## Advanced options

### PREDICTED VALUES

#### Effective dose

50 %

#### Reported as

Container / Effective Dose

#### Y values

1.5;2

You can specify up to 6 response values, separated by semicolons.

## Effective dose estimates

Preparation	Units	Effective Dose (ED)		Relative To Estimate (%)	
		Estimate	(LCL, UCL)	Rel. To Est.	(LCL, UCL)
Standard	IU/ED50	0.00539071	(0.00521456, 0.00557304)	100	(96.73, 103.38)
Sample 1	IU/ED50	0.00369516	(0.00357478, 0.00381967)	100	(96.74, 103.37)

Confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

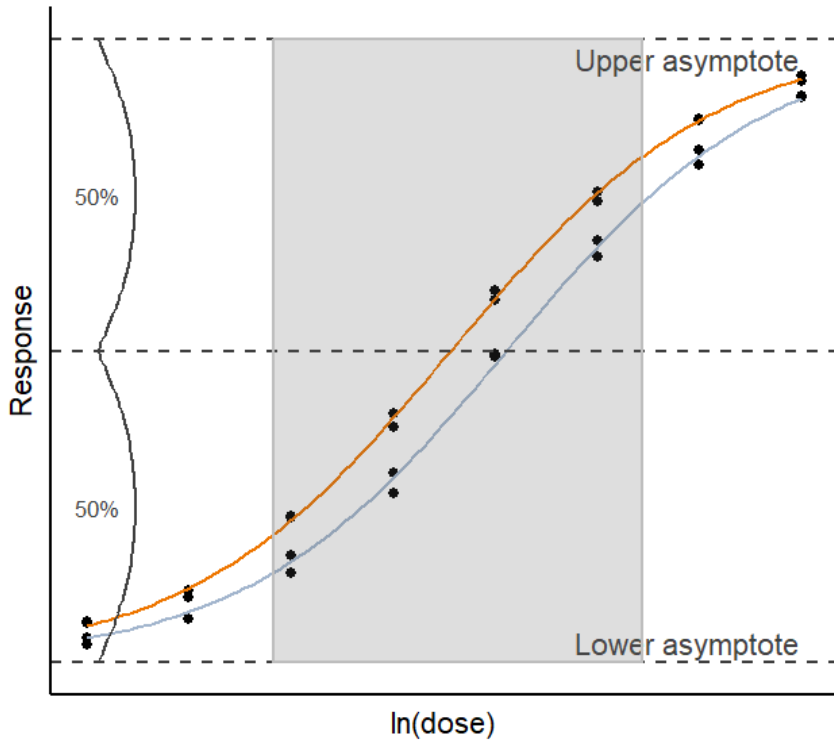
## Inverse predictions

Preparation	Units	y-value(s)			
		1.5		2	
		Estimate	(LCL, UCL)	Estimate	(LCL, UCL)
Standard	IU	0.00441394	(0.00426822, 0.00456375)	0.00796270	(0.00769247, 0.00824648)
Sample 1	IU	0.00302561	(0.00292584, 0.00312811)	0.00545817	(0.00527405, 0.00565138)

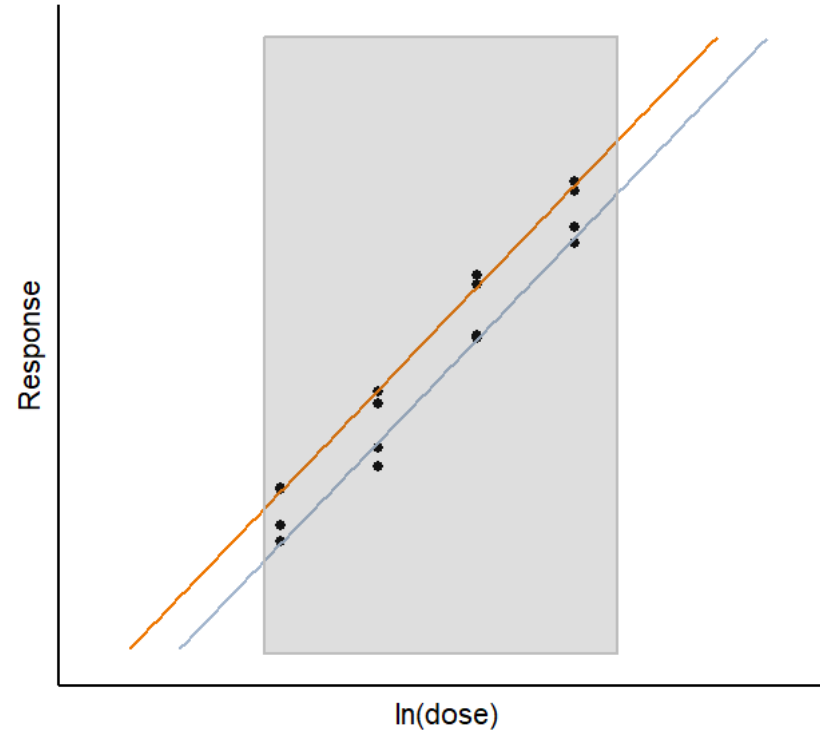
Confidence limits (in brackets) calculated for a 95% confidence level (advanced options).

# Parallel lines model as special case of 4PL

4PL model



Parallel line model



Potency estimates

Preparation	Units	Potency	
		Estimate	(LCL, UCL)
Sample 1	IU/ml	0.584197	(0.555852, 0.614008)

Potency estimates

Preparation	Units	Potency	
		Estimate	(LCL, UCL)
Sample 1	IU/ml	0.572008	(0.533897, 0.613680)

New feature in Online version

## Subset analysis

may help in dose selection

Model

Sigmoid curves (4-PL, ln dose) ▼

**Parallel lines (ln dose)**

Slope ratio (dose)

Sigmoid curves (4-PL, ln dose)

Asymmetric sigmoid curves (5-PL, ln dose)

Exponential curves (ln dose)

*Change model in Wizard*

*Subset set-up in Advance options*

Subset

Shift & Drop ▼

Selection criterion

Slope steepness ▼

**Slope steepness**

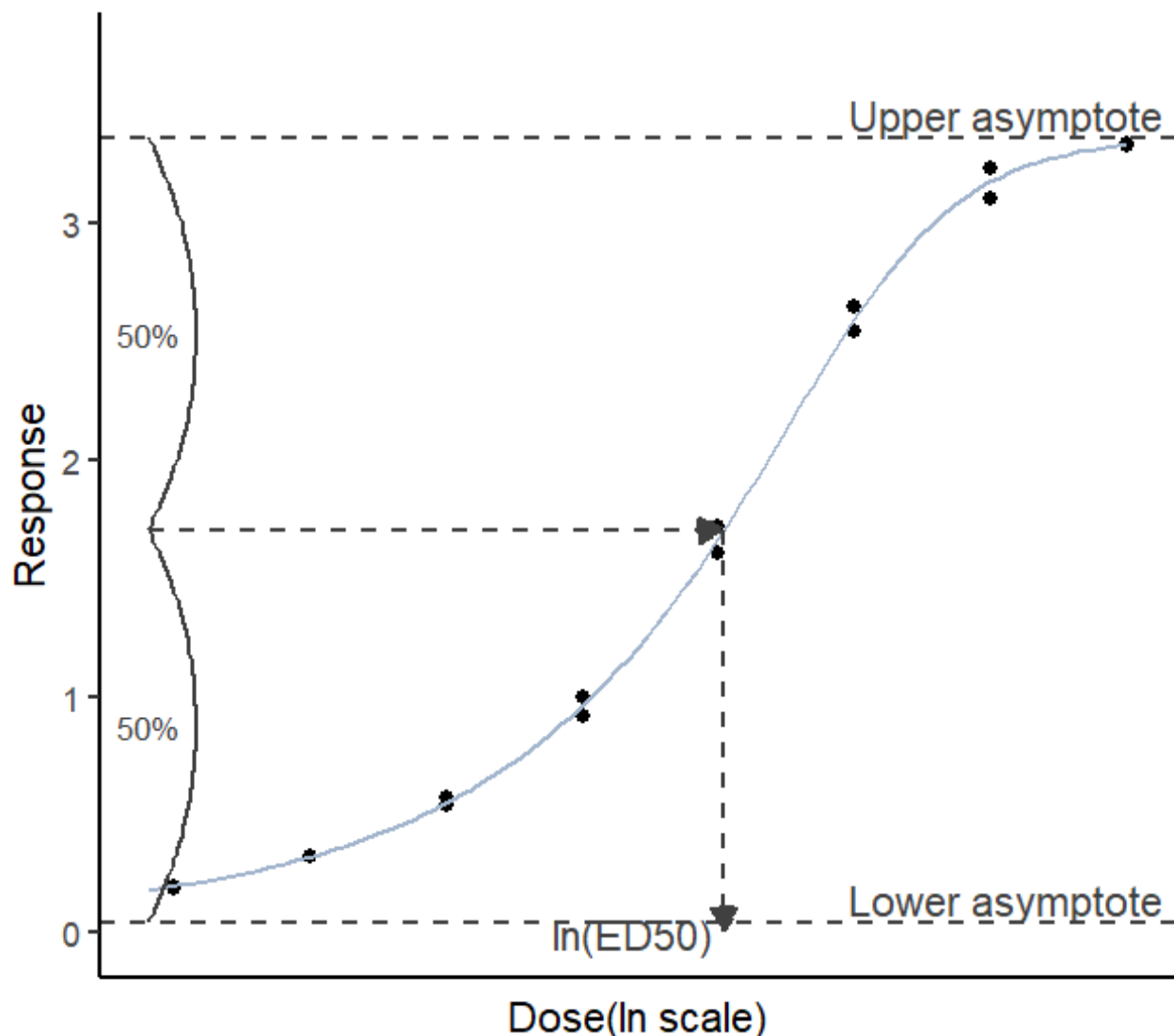
Coefficient of determination (R<sup>2</sup>)

# Content

---

- Introduction
- Parallel-line analysis
- Slope-ratio analysis
- 4-parameter logistic model
- **5-parameter logistic model**
- 3-parameter exponential model

# 5PL – dose-response relationship



## Asymmetrical S-shaped curve

- One to two concentrations for each asymptotes
- Three to four concentrations for middle part of the curve

$$Response = D + \frac{A - D}{[1 + \exp(B * (\ln(dose) - C))]^G}$$

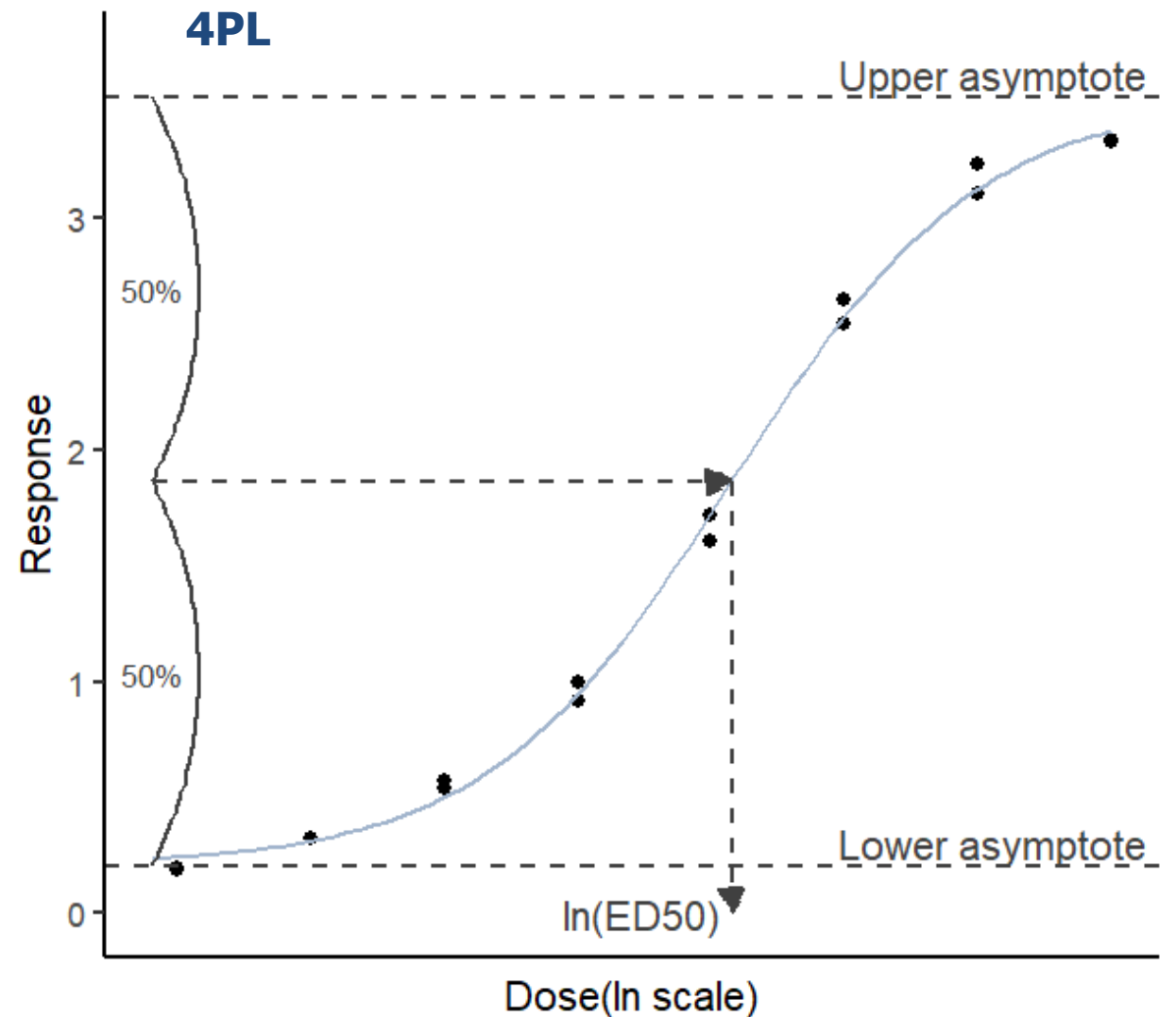
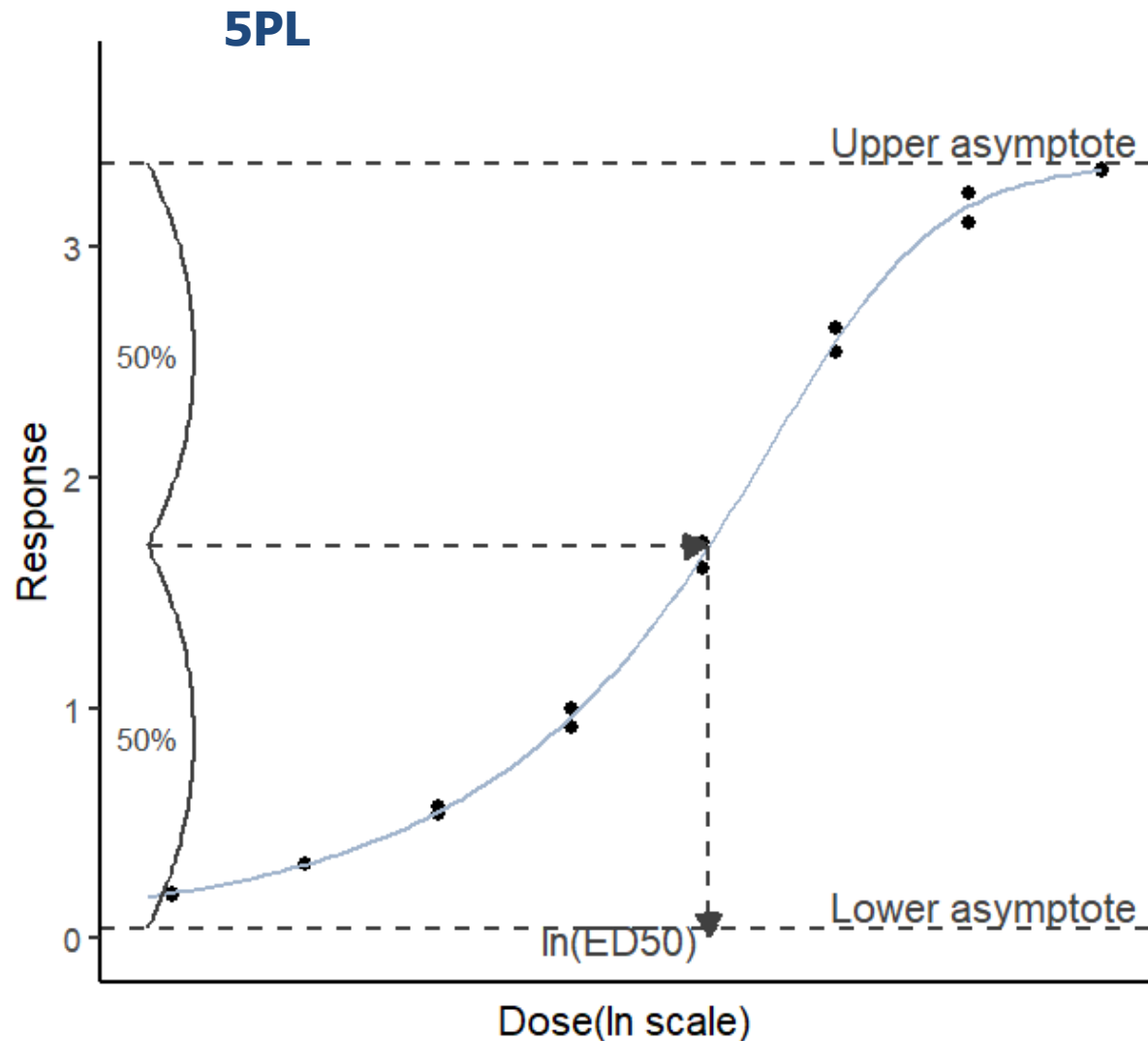
where *D*: upper asymptote  
*A*: lower asymptote  
*C*: location parameter ( $\neq ED50$ )  
*B*: Slope  
*G*: Asymmetry factor

Assays: ELISA or cell-based potency assays



# 5PL – 4PL comparison

Model	R <sup>2</sup>	Lower asymptote	Upper asymptote	ED50
5PL	0.994	0.048	3.36	0.244 IU
4PL	0.988	0.207	3.52	0.261 IU



# 5PL – Creation and evaluation in CombiStats online

## New record

Type

Assay

Name

Assay1\_5PL

To folder

David

Elena

My folder

Assay

Multiple-dose

Type of design

Completely randomised

Response variable

Quantitative

Model

Asymmetric sigmoid curves (5-PL, In dos

Preparations

2

Max doses

5

Max replicates

3

Cancel

Create

Model = Asymmetric sigmoid curves (In dose)

Analysis options are the same as for 4PL model except for linearising transformation

Linearising transformation

Logit

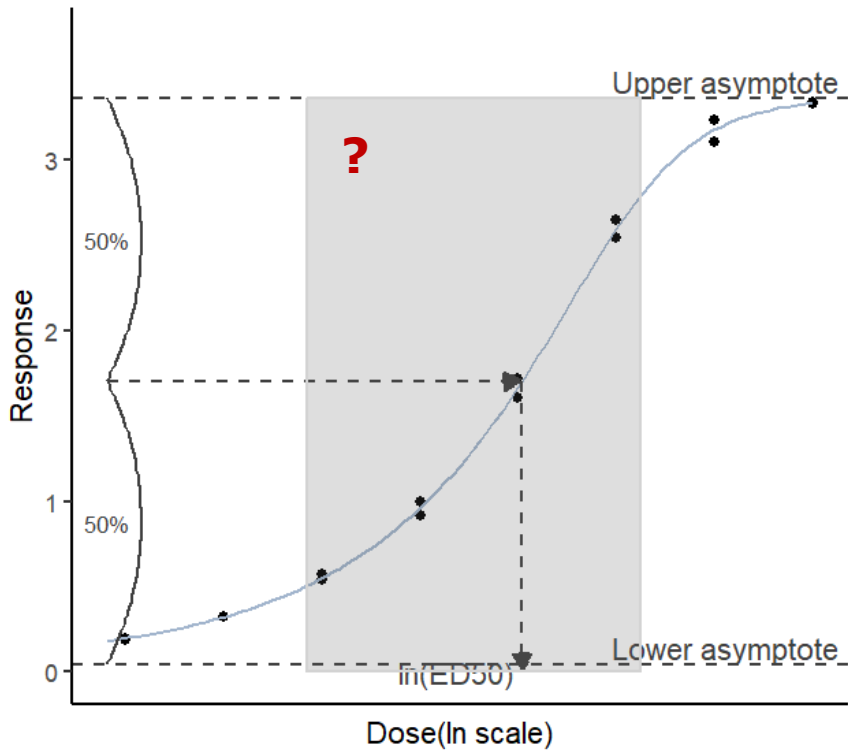
Probit

Logit

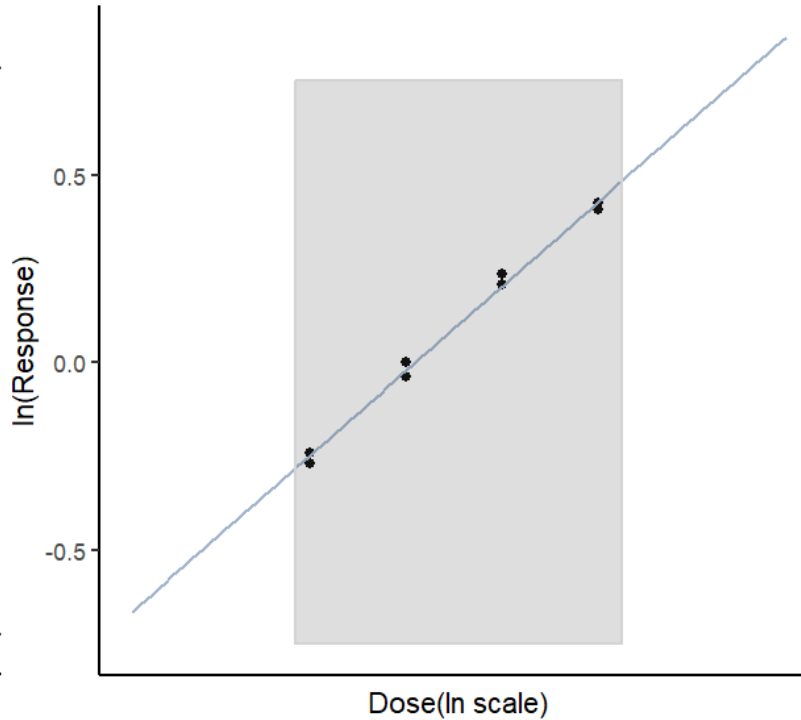
# Parallel line model for routine testing

Middle section (section of the steepest slope) is often not linear for asymmetrical sigmoid models. An appropriate transformation to be applied for parallel line model.

## 5PL – middle section **not linear**



## PL - transformed response



New feature **Subset analysis** may help in dose selection

**Model**

Asymmetric sigmoid curves (5-PL, ln dose) ▼

Parallel lines (ln dose)

---

**Transformation**

No transformation:  $y'=y$  ▼

No transformation:  $y'=y$

Inverse:  $y'=1/y$

Logarithm:  $y'=\log(y)$

*Change model and transformation in Wizard*

---

**Subset**

Shift & Drop ▼

**Selection criterion**

Slope steepness ▼

Slope steepness

Coefficient of determination ( $R^2$ )

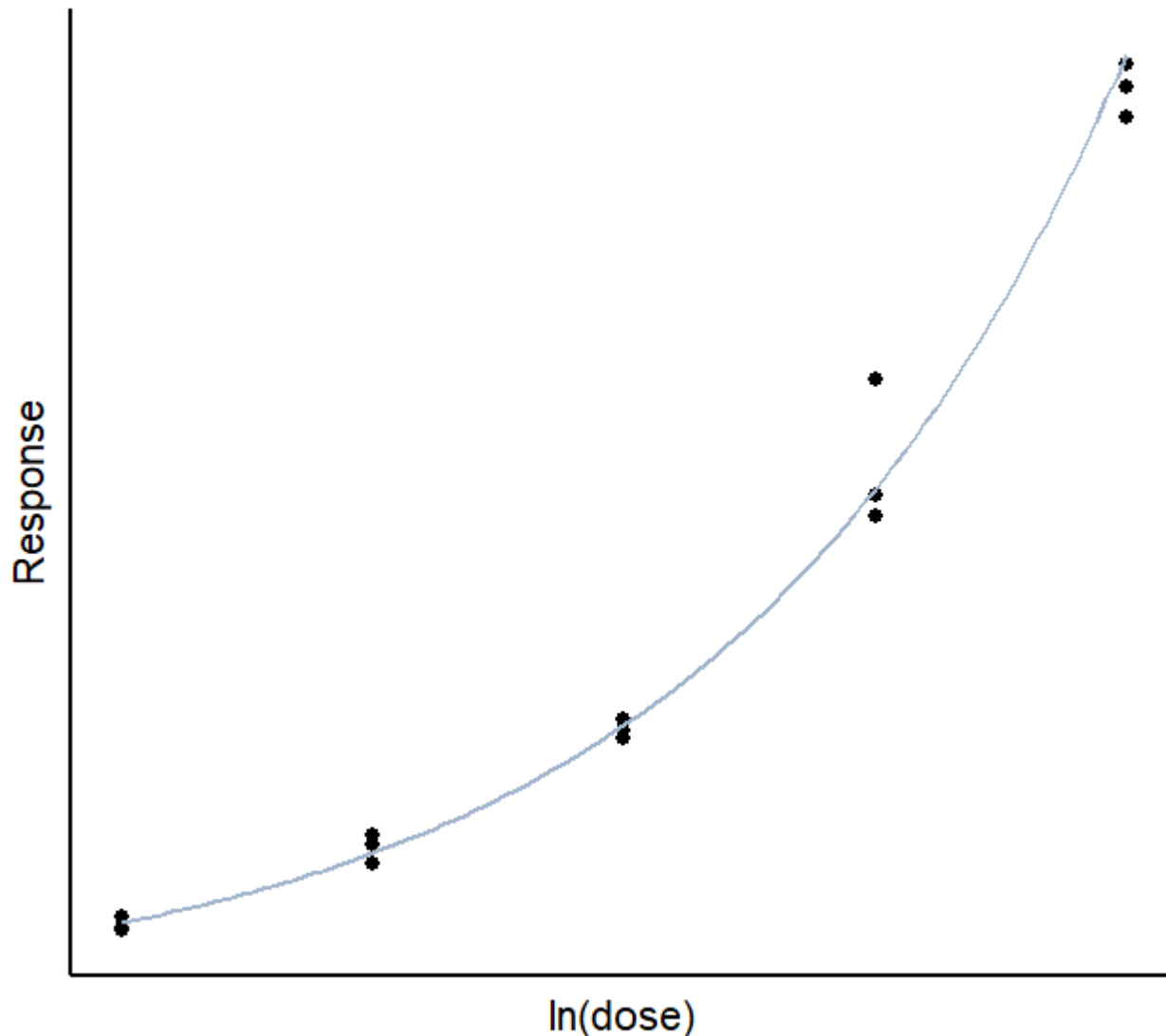
*Subset set-up in Advance options*

# Content

---

- Introduction
- Parallel-line analysis
- Slope-ratio analysis
- 4-parameter logistic model
- 5-parameter logistic model
- **3-parameter exponential model**

# 3PM – dose-response relationship



Modelling exponential growth

No upper asymptote as in 4PL and 5PL

$$Response = D + A * \exp(B * (\ln(dose) - C))$$

where *D*: addition

*A*: multiplication

*C*: location parameter

*B*: slope parameter

Assay:

Hepatitis B vaccine (A3.29),

Yellow fever vaccine (A3.23), plaque forming units

# 3PM – modelling exponential growth

Usually, variability of response increases with higher response values and needs to be stabilised.

Case 1: responses are based on counting of events in a Poisson or Poisson-like process

⇒ Weighted regression (1/m)

Case 2: responses are based on exponential distribution

⇒ Weighted regression (1/m<sup>2</sup>)

$$Response = D + A * \exp(B * (\ln(dose) - C))$$

If D=0 and A=1

$$Response = \exp(B * (\ln(dose) - C))$$

$$\begin{aligned} \ln(Response) &= \ln(\exp(B * (\ln(dose) - C))) \\ &= B * (\ln(dose) - C) \\ &= B * \ln(dose) - B * C \\ &= -B * C + B * \ln(dose) \end{aligned}$$

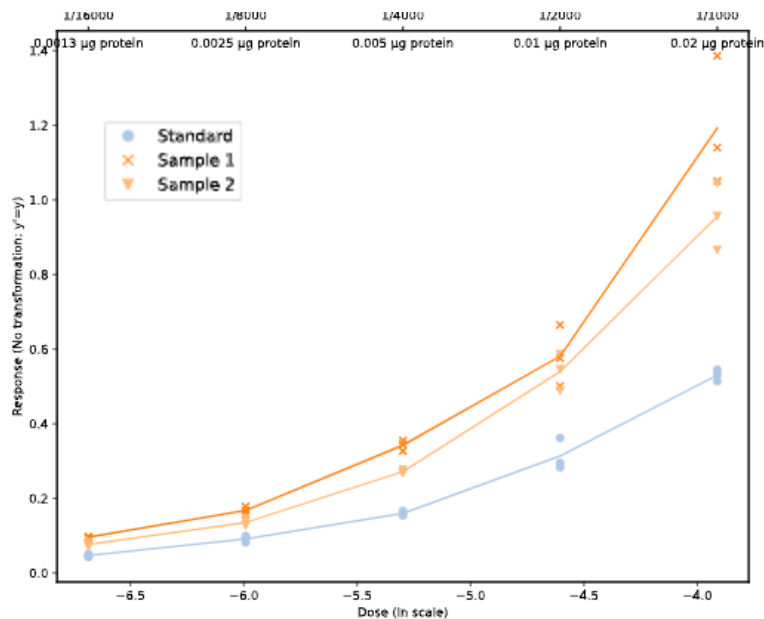
intercept slope

# Example: alternative to PL with log-transformation

Hepatitis B vaccine (A3.29)

Standard and two test preparations  
5 doses

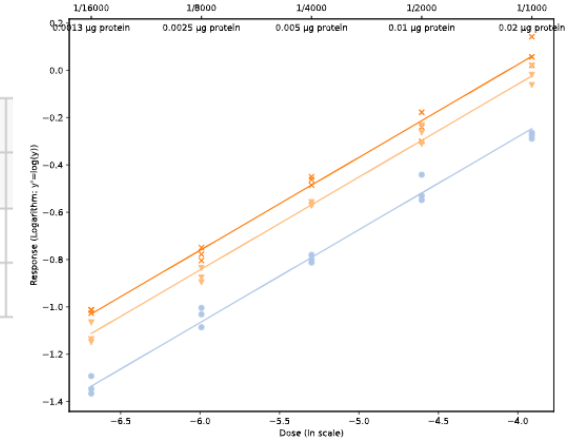
Average plot (no transformation)



PL model with log-transformation

Potency estimates

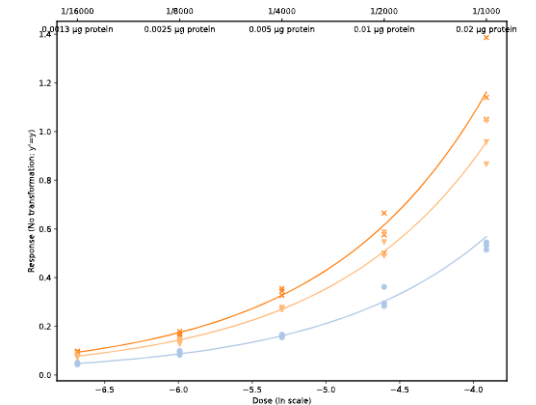
Preparation	Units	Potency	
		Estimate	(LCL, UCL)
Sample 1	µg protein/ml	43.5762	(40.4020, 47.0668)
Sample 2	µg protein/ml	35.2553	(32.7374, 38.0062)



3PL weighted regression (D=0, A=1, weight=1/m<sup>2</sup>)

Potency estimates

Preparation	Units	Potency	
		Estimate	(LCL, UCL)
Sample 1	µg protein/ml	43.5676	(40.4720, 46.9635)
Sample 2	µg protein/ml	35.2206	(32.7673, 37.8948)



# 3PM – Creation and evaluation in CombiStats online

New record

Model = Exponential curves (In dose)

<b>Type</b> Assay	<b>Assay</b> Multiple-dose	<b>Type of design</b> Completely randomised	<b>Response variable</b> Quantitative	<b>Model</b> Exponential curves (In dose)
<b>Name</b> Assay1_3PM	<b>Preparations</b> 2	<b>Max doses</b> 5	<b>Max replicates</b> 3	
<b>To folder</b> David Elena My folder	<b>Cancel</b> <b>Create</b>			

## Advanced options

### Wizard

<b>Model</b> Exponential curves (In dose)
<b>Transformation</b> No transformation: $y'=y$
<b>Variance</b> Observed residuals

<b>FIXED PARAMETER</b>
<b>Slope</b> 1.0
<b>Addition</b> 0.0
<b>Multiplication</b> 100.0

<b>REGRESSION TYPE</b>
<b>Weighting</b> Unweighted regression
Unweighted regression
Weighted regression (1/m <sup>2</sup> )
Poisson regression (1/m)
User-defined (w=...)

Analysis options are similar to 4PL model without linearizing transformation choice





# Thank you for your attention

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